

Margin Requirements, Risk Taking, and Multifactor Models

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Abstract

When investors anticipate the Fed increasing margin requirements, they bid up the riskier stocks in the long legs of hedge portfolios associated with the market, HML, and SMB factors relative to the less risky stocks in the short legs. Following such a policy change, the returns on these hedge portfolios decline, implying lower subsequent compensation for bearing the risk associated with these three factors. In contrast, margin requirements are unrelated to returns on the momentum factor. Our evidence suggests that investors adjust their risk exposures to the market, SMB, and HML factors when leverage constraints are changed, but not momentum.

JEL Classification : G12, G14, G41.

Key Words: Asset pricing, CAPM, multifactor models, security market line, leverage constraints, margin requirements, risk premia.

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I. Introduction

According to Black (1972) and Frazzini and Pedersen (2014), when investors face the prospect of tighter leverage constraints, they may respond by overweighting riskier stocks to obtain their desired level of overall risk that cannot be achieved through leverage. This theory implies two divergent predictions for the initial versus subsequent price response of assets with more or less risk. First, the overweighting of more risky assets should initially drive up their prices relative to less risky assets, in anticipation of the tighter leverage constraints. Second, following this price increase, expected future returns on more risky assets should drop relative to less risky assets, implying a subsequent decline in the compensation for bearing risk.

We contribute to the emerging literature on this theory by thoroughly investigating the two predictions above, in the context of multifactor models. Following Jylha (2018), we examine the 22 changes in margin requirements by the Federal Reserve over the period, 1934 – 1974.¹ We expand the analysis to include HML, SMB, and UMD from the multifactor models of Fama and French (1993, 1995, and 1996) and Carhart (1997), as well as a market-based hedge portfolio that is long stocks with a high beta and short stocks with a low beta (labeled MBeta). In addition, we separately analyze the subsets of stocks with more risk versus less risk in the long and short legs of these factor hedge portfolios, as well as the hedge portfolios themselves.²

The work of Black (1972) and Frazzini and Pedersen (2014) has inspired an emerging literature that empirically investigates various implications of this theory. Our study addresses two important gaps in this literature. First, prior to our paper, these two predictions about the return dynamics of assets with more versus less risk have not yet been thoroughly explored. Most

¹ Jylha (2018) shows that the 22 changes in margin constraints over this period significantly affected investors' access to leverage, but were largely uncorrelated with financial market and macroeconomic conditions at the time.

² MBeta is the negative of the betting-against-beta (BAB) factor of Frazzini and Pedersen (2014), constructed to be consistent with HML and SMB where the riskier (high beta, value, or small) stocks appear in the long leg.

prior studies rely on the betting-against-beta (BAB) factor of Frazzini and Pedersen (2014), which is long leveraged low-beta assets and short high beta assets. These studies do not separately examine the subsets of stocks with more versus less risk (i.e., a higher versus lower beta), and they yield mixed results. For example, Frazzini and Pedersen (2014) find that tighter funding constraints (proxied by a higher TED spread) are associated with a decline in returns on the BAB factor in the same month, which implies increasing prices of assets with more risk versus less risk, consistent with the first prediction. However, they also find that the prices of assets with more versus less risk continue to increase in subsequent months, contrary to the second prediction. Boguth and Simutin (2018) consider alternative means to analyze leverage constrained investors. They show that the average market beta of actively managed mutual funds, which face binding leverage constraints, predicts returns on BAB in a manner consistent with the second prediction. Similarly, Lu and Qin (2019) measure the shadow cost of leverage constraints from data on leveraged funds, and examine its dynamic relation with BAB returns.

While these three studies analyze how leverage conditions are related to returns on the BAB factor, the theory implies that investor demand for the riskier (i.e., high beta) stocks in this hedge portfolio should drive the results. Thus, a comprehensive examination of both predictions of this theory requires separately analyzing the return dynamics of stocks with a high beta versus stocks with a low beta, rather than just a hedge portfolio involving both sets of assets. On another level, despite its broad impact and pervasive use in the literature, Novy-Marx and Velikov (2018) show that returns to the BAB factor are driven by non-standard leverage and weighting schemes used in its construction which effectively overweight micro-cap and nano-cap stocks. This concern calls into question whether the evidence in these three studies can be generalized.³

³ While our MBeta portfolio is the negative of the BAB factor of Frazzini and Pedersen (2014), we do not apply the weighting or leverage schemes used to construct their BAB factor, which concern Novy-Marx and Velikov (2018).

Jylha (2018) takes a different approach and analyzes the slope of the CAPM security market line (SML) around the 22 changes in margin requirements made by the Fed over the period, 1933 – 1974. He shows that higher margin requirements are associated with a weaker relation between expected future returns and the return sensitivity of the market factor. This evidence is consistent with the second prediction from this theory, implying a flatter SML and thus lower subsequent compensation for bearing risk. However, while Jylha (2018) analyzes the SML under different margin regimes, he does not directly examine the dynamic behavior of stock returns or the first prediction of this theory. Moreover, like the other papers cited above, Jylha (2018) does not separately examine the return dynamics of stocks with a high versus a low beta, which is necessary for a comprehensive examination of both predictions from the theory.

The second gap in this emerging literature arises from its reliance on a stock's market beta as the sole measure of risk. These studies assume that investors use the CAPM as the relevant model of risk to make capital allocation decisions. However, in the past three decades, several additional factors have been proposed to help explain the cross section of expected stock returns. While empirically motivated, these factors may proxy for unobserved state variables that describe time variation in risks associated with the investment opportunity set. Hence, investors may also prefer to invest in alternative risky assets associated with these factors to increase their risk when facing leverage constraints, which would affect the prices of these alternative factors.⁴

This argument is similar in spirit to Kojien and Yogo (2019), who develop an asset pricing model where the optimal mean-variance portfolio varies across investors due to heterogeneous beliefs. They assume that stock returns have a factor structure where expected

⁴ Fama and French (1993), Liew and Vassalou (2000), Lettau and Ludvigson (2001), Vassalou (2003), and Petkova (2006) interpret the returns on these factors as risk premia. Similarly, Merton (1973) and Ross (1976) emphasize that certain characteristics of firms and the opportunity set faced by investors reflect multifactor risk premia.

returns and factor loadings depend on the firm's characteristics. Under this factor structure, the optimal portfolio simplifies to a demand function that depends on the firm's characteristics (such as market beta, book-to-market, size, investment, and profitability), as well as *latent demand* (i.e., unobserved sources of demand in the marketplace).

In our setting, although leverage constraints are not explicitly modelled in Kojien and Yogo (2019), the overweighting of risky assets due to changes in margin requirements might be viewed as a source of such latent demand for firm characteristics that capture risk. Accordingly, variation in latent demand due to changes in leverage constraints could affect the relative returns on assets with more or less risk underlying the long and short legs of factor hedge portfolios other than the market, and could thereby affect the pricing of these alternative sources of risk. Ultimately, it is an empirical question as to whether leverage constrained investors act to achieve a higher level of multiple aspects of risk by investing in portfolios with greater exposure to these other factors, as well as the market.⁵

Figure 1 provides a first glance at our main results. We plot the mean daily cumulative abnormal returns for the long and short legs of each factor hedge portfolio, over the 181 days around the 12 increases or 10 decreases in margin requirements during the period, 1934 – 1974. On the left side of Panels A – C in Figure 1, when margin constraints are *increased*, the more risky stocks in the long legs of the first three factor portfolios (i.e., high beta stocks, value stocks, and small stocks) are bid *up* prior to day 0, relative to the less risky stocks in the short legs. After

⁵ We focus on the Fama and French (1993) three-factor model and the Carhart (1997) four-factor model, rather than the five-factor model of Fama and French (2015), because dependable data are unavailable for the investment and profitability factors since 1934, and these two factors do not display priced risk or return predictability before 1963. We do not suggest that the Fama and French three-factor or Carhart four-factor model is the 'correct' asset pricing model. We only wish to examine whether investors respond to changes in leverage constraints by bidding up or down the stocks in the long versus short legs of these four factor portfolios in a manner consistent with this theory.

day 0, returns on the more risky stocks stop diverging from the less risky stocks, implying a subsequent decline in the expected returns on these factor hedge portfolios.

Importantly, these return dynamics are reversed for the first three factors (MBeta, HML, and SMB) around *decreases* in margin requirements, on the right side of Panels A - C in Figure 1. Now, when leverage constraints are relaxed, the more risky portfolios (i.e., high beta, value, and small stocks) are initially bid *down* relative to less risky stocks, before rising as day 0 approaches to reveal higher subsequent returns. For these three factors, the evidence in Panels A – C is consistent with the fundamental premise of this theory, suggesting that an impending increase (or decrease) in margin requirements prompts investors to shift away from (or towards) their optimal portfolios, by buying (or selling) riskier assets relative to safer assets.

In contrast, for momentum the return dynamics are not reversed for increases versus decreases in margin requirements on the left and right sides of Panel D in Figure 1. This outcome deviates from the fundamental premise in Black (1972) and Frazzini and Pedersen (2014). Whether margin requirements are increased or decreased, the winner stocks in the long leg of the UMD portfolio continue to drift up while the loser stocks in the short leg continue to drift down. This evidence suggests that investors do not rely on the momentum factor as a means to realign their portfolios toward more risky assets when leverage constraints are tightened and toward less risky assets when they are relaxed.⁶

It is noteworthy that, in Panels A – C of Figure 1, the price response begins 20 to 60 days in advance of the actual change in margin requirements on day 0. This result indicates that the market anticipated these policy changes well in advance, suggesting that the Fed often managed

⁶ These results do not imply that changes in margin requirements have no impact on winner or loser stocks, but only that winner and loser stocks behave similarly when margin requirements are either increased or decreased, which is contrary to the fundamental premise from the theory of Black (1972) and Frazzini and Pedersen (2014).

expectations by disclosing its intention to change margin requirements early.⁷ Consistent with this observation, Appendix A provides several quotes from the *Wall Street Journal* published prior to these policy changes, which document that the Fed frequently discussed (and the market responded to) its intention to increase or decrease margin requirements well ahead of time.

In our first set of formal tests, we expand upon the preliminary analysis of returns in Figure 1. We begin by directly investigating the *first prediction* to analyze how the factor portfolio returns vary in the months *prior to* future changes in margin requirements, while controlling for other variables that also affect returns. Consistent with the first prediction and the evidence in Figure 1, returns on the first three factor portfolios (MBeta, HML, and SMB) are *positively* related to *anticipated future* changes in margin requirements. That is, the returns on these three hedge portfolios rise in the months before an increase in margin requirements and drop before a decrease in margin requirements. Moreover, these return dynamics are driven by significant changes in returns on the riskier stocks in the long leg of each factor portfolio (i.e., high beta stocks, value stocks, and small stocks). In contrast, returns on the winner and loser portfolios are similar to each other in the months before a change in margin requirements, so that the combined momentum (UMD) portfolio does not significantly rise before an increase in margin requirements or drop before a decrease in margin requirements.

Next, we directly investigate the *second prediction* to examine whether this behavior reverses *following* the policy change. Now, for the first three factors (MBeta, HML, and SMB), we find a significant *negative* relation between hedge portfolio returns and *past* margin requirements. That is, these three hedge portfolio returns drop (rise) in the months *after* an

⁷ In contrast to Panels A – C, the prices of winner (loser) stocks in Panel D begin drifting up (down) on day -90, as soon as we start tracking prices. We also note that these momentum stocks continue to drift up or down whenever we start tracking prices, while the price response in Panels A – C does not change if we start tracking prices earlier.

increase (decrease) in margin requirements. These results are also driven by the riskier stocks in the long leg of each factor portfolio (i.e., high beta, value, and small stocks). This evidence is consistent with the second prediction and Figure 1, implying that an increase (decrease) in margin requirements is associated with lower (higher) *subsequent* hedge portfolio returns in the following months, which persist for up to twenty months later. Once again, the analogous return dynamics for momentum (UMD) do not provide similar support for the second prediction.

In our second set of tests, we investigate whether leverage constraints affect the compensation for other aspects of risk embodied in multifactor models, beyond the market. In particular, we examine the time series relation between lagged margin requirements and the monthly intercepts or slopes of the SML analogues (i.e., the relations between expected returns and return sensitivities) pertaining to the HML, SMB, and UMD factors, as well as the market factor. Following Jylha's (2018) analysis of the SML based on the CAPM, these monthly SML analogues are obtained from two-stage cross sectional estimation of the Fama-French (1993) three-factor and Carhart (1997) four-factor models for each month over the period, 1934 – 1975.

We find that margin requirements in month $t-1$ are positively related to the intercept of the SML analogues from both the three-factor and four-factor models in month t , and negatively related to the slopes for the first three factors (i.e., the market, HML, and SMB). For these three factors, this evidence is also consistent with the second prediction of the theory in Black (1972) and Frazzini and Pedersen (2014), indicating that higher margin requirements are associated with flatter SML analogues in the following month, and thus lower subsequent compensation for bearing risk. In contrast, lagged margin requirements are unrelated to the slope of the SML analogue for momentum (UMD). We also document that these findings are robust when we use alternative test assets, or analyze factors that are constructed to be market-neutral, or control for

other influences such as the cost of leverage, aggregate disagreement, and short sale constraints. These tests address the potential concern that our results could be driven by variables that may be associated with both margin requirements and the compensation for risk-taking by investors.⁸

A potential alternative explanation for our findings is that margin requirements may affect the HML and SMB factor returns through a mispricing channel, rather than through risk, by restricting the capital available to noise traders and arbitrageurs, respectively.⁹ First, according to this view, if higher margin requirements *limit* the capital available to *noise traders*, we would expect *less* mispricing and *lower* returns to the HML and SMB factors following an increase in margin requirements.¹⁰ Such a negative relation is also consistent with the second prediction from this theory. However according to this view, since investors rarely sell short, leverage constraints should mainly limit the buy side behavior of noise traders, which should reduce the high prices of stocks in the overvalued short legs of the HML and SMB portfolios (i.e., growth stocks and large stocks, respectively).¹¹ But this outcome is contrary to our findings. Instead, we find that higher margin requirements have a stronger effect on the riskier stocks in the long legs of the SMB and HML factors (i.e., value stocks and small stocks).

Next, to the extent that higher margin requirements *limit arbitrageurs* from exploiting mispricing opportunities, we would expect *more* mispricing, which should lead to *higher* returns

⁸ Prior literature identifies several additional factors that may also affect the slope of the CAPM security market line, including inflation (Cohen, Polk, and Vuolteenaho, 2005), aggregate investor disagreement (Hong and Sraer, 2016), investor sentiment (Antoniou, Doukas, and Subrahmanyam, 2016), speculative capital (Huang, Lou, and Polk, 2016), macroeconomic announcements (Savor and Wilson, 2014), institutional trading (Karceski, 2002; Buffa, Vayanos, and Woolley, 2014; Christoffersen and Simutin, 2017; and Boguth and Simutin, 2018), and the cost of leverage (Cohen, Polk, and Vuolteenaho, 2005; and Jylha, 2018). We account for these variables in our analysis.

⁹ See Golubov and Konstantinidi (2018) for an excellent review of this literature pertaining to the value premium.

¹⁰ For example, see De Bondt and Thaler (1985), Haugen (1994), and Lakonishok, Shleifer, and Vishny (1994).

¹¹ For example, see Barber and Odean (2008) and Odean (1999). In addition, Jylha (2018, p. 1314) notes that, “short interest was very low throughout the sample period. The aggregate short interest ratio varied between 0.03% and 0.19%, with an average of 0.08%.”

on the HML and SMB factors (i.e., a positive relation between margin requirements and later factor returns). However, this outcome is also contrary to our findings of a negative relation.

On the other hand it is possible that, when arbitrageurs are forced to curtail their activity following an increase in margin requirements, the deviation of prices from fundamentals may persist or even grow due to the unabated actions of noise traders.¹² For example, in the short term value stocks may become even more underpriced while growth stocks become even more overpriced, implying a negative return on the long-short HML portfolio. However, our evidence that value stocks are bid up (or down) relative to growth stocks *prior to* increases (or decreases) in margin requirements is inconsistent with this argument, since one would expect an inverse relation. Furthermore, while it is possible that prices may deviate further from fundamentals in the short run following an increase in margin requirements, due to reduced arbitrage activity, they should eventually converge back toward fundamentals. We also test this implication, but we find no evidence of an eventual reversal from a negative relation to a subsequent positive relation over the following three years. Thus, our findings are unlikely to be explained by mispricing.

II. Related Literature

Our analysis contributes to several strands of literature. First, we shed new light on the emerging literature that examines the dynamic relation between borrowing constraints and asset prices. While Jylha (2018) finds a flatter SML following higher margin requirements, he does not consider the multiple aspects of risk embodied in multifactor models. Nor does he directly examine returns to the factor portfolios around changes in margin requirements, let alone the

¹² See Campbell and Kyle (1993) and De Long, Shleifer, Summers, and Waldman (1990) for a discussion of how limited arbitrage activity may allow deviation of prices from fundamentals to persist or grow due to noise trader risk.

long and short legs of these hedge portfolios. In addition, measuring the slope of the SML in a two-stage analysis is inherently noisy and highly subject to the time period analyzed.¹³

We suggest that the theory can be more effectively tested by directly examining the return dynamics of assets with more risk or less risk around changes in margin requirements. Among other things, Frazzini and Pedersen (2014) consider these return dynamics by analyzing the relation between the TED spread and returns on their BAB factor. However, they find that the prices of assets with more versus less risk continue to increase after a tightening of funding conditions, contrary to the second prediction from their model. Boguth and Simutin (2018) and Lu and Qin (2019) consider alternative means to analyze risk-taking behavior by constrained investors, but these studies all rely on the BAB factor and do not separately analyze assets with more or less risk. Our analysis provides strong support for both predictions of this theory regarding the return dynamics of assets with more risk versus assets with less risk, and does so in a multifactor setting, thereby complementing and extending these prior studies.

Second, we also shed new light on the ongoing debate about whether the pricing of these multiple factors reflects compensation for risk or market mispricing. Interpretation of our results with respect to the Frazzini and Pedersen (2014) model of leverage constraints implies that, in addition to high beta stocks, constrained agents would prefer to buy value or small-cap stocks to achieve higher expected returns, since they are more risky than growth or large-cap stocks. In this context, the return premium associated with the HML and SMB factors should represent, at least partially, compensation for the greater risk associated with value stocks and small-cap stocks. This interpretation is also in accord with the recent body of work that attempts to

¹³ For discussion of these concerns, see Black, Jensen, and Scholes (1972), Cochrane (2001), Fama and MacBeth (1973), Jensen (1972), and Miller and Scholes (1972).

empirically identify ‘true risk factors.’ This literature suggests that, while SMB and HML satisfy the necessary conditions to be considered as risk factors, momentum does not.¹⁴

On the other hand, if risk-taking behavior like that modeled in Frazzini and Pedersen (2014) cannot explain the returns to momentum (which averaged 0.7% per month over our sample), then perhaps an alternative explanation based on market mispricing and unexploited arbitrage opportunities is more likely to apply to momentum. If sophisticated investors were unaware of these momentum returns as early as the 1930s, then they would not have actively traded against this phenomenon and thereby counteracted any such mispricing opportunities.¹⁵

Third, our analysis draws upon the broad literature that attempts to understand cross sectional variation in expected stock returns. Our analysis suggests that leverage constraints represent one important source of the failure of multifactor models to adequately explain the cross section of expected returns.¹⁶ In particular, the positive relation between margin requirements and the intercept of these SML analogues implies a higher unconditional return for a portfolio with zero exposure to each factor, when margin requirements are higher. This outcome suggests that these factors fail to adequately explain variation in the performance of the test assets analyzed when leverage constraints vary.

Fourth, our results also offer an alternative perspective on whether the findings in Jylha (2018) can be explained by investor demand for lottery-like payoffs. According to this argument,

¹⁴ For example, Moskowitz (2003) argues SMB satisfies the condition to be a risk factor and HML is close to satisfying this condition, but momentum is not. Similarly, based on Cochrane (2001), Charoenruek and Conrad (2008) argue that, while SMB and HML satisfy the necessary condition to be a risk factor, momentum does not. They also find that the mean/volatility relation for the momentum factor has the wrong sign, suggesting that its return predictability might be due to unexploited arbitrage opportunities associated with mispricing, rather than risk.

¹⁵ The value investment strategies of Graham and Dodd (1934) have been well known since the 1930’s, while the size anomaly was first documented by Banz in 1981, and the momentum strategy was first published by Jegadeesh and Titman in 1993. Consistent with this view, Daniel, Hirshleifer, and Subrahmanyam (1998), Barberis, Shleifer, and Vishny (1998), and Hong and Stein (1999) provide behavioral explanations for momentum based on mispricing.

¹⁶ As critiqued by Lewellen, Nagel, and Shanken (2010), the apparent strong explanatory power of these multifactor models measured by a high R^2 and small pricing errors may not truly support the success of these models.

rather than leverage constraints, investor demand for lottery-like stocks (e.g., MAX) drives the lower expected returns on such high beta stocks.¹⁷ Jylha (2018) argues that margin requirements are unlikely to be related to investors' preferences for lottery-like payoffs. Similarly, our finding that the HML and SMB factors are also affected by leverage constraints would be difficult to explain using an argument based on lottery preferences. For example, according to Bali, Brown, Murray, and Tang (2017), unlike market beta, the underlying characteristics of the HML and SMB factors (i.e., book-to-market and size) survive a horse race with MAX. Hence, we conclude that our findings are not likely to be explained by investor demand for lottery-like stocks.¹⁸

III. Data and Variables

III.A. Changes in Margin Requirements over the Period, 1934 - 1975

The Federal Reserve changed margin requirements 22 times between October 1934 and January 1974. In Table I we list the dates of these changes, along with the minimum level of margin required at each change (Federal Reserve Board, 1976b, Table 12.22).¹⁹ Jylha (2018) finds that margin credit and past market returns were positively related with the Fed's decisions to change margin requirements over this period. However, other macroeconomic and financial market conditions were unrelated to margin requirements, including stock market volatility, market skewness, share turnover, the price-dividend ratio, inflation, and the money supply (M1). Thus, Jylha (2018) argues that the level of margin required over this period was not merely a projection of prevailing market and macroeconomic conditions, and these changes provide a

¹⁷ See Asness, Frazzini, Gormsen, and Pedersen (2018), Bali, Brown, Murray, and Tang (2017), Bali, Cakici, and Whitelaw (2011), Barberis and Huang (2008), and Brunnermeier, Gollier, and Parker (2007). Also, Liu, Stambaugh, and Yuan (2018) contend that the lower expected returns on high beta stocks are driven by idiosyncratic risk.

¹⁸ Another related strand of literature examines the effect of margin regulation on market risk (Ferris and Chance, 1988, Kupiec, 1989, Schwert, 1989, and Hsieh and Miller, 1990). The main consensus in this literature is that margin requirements have no impact on market volatility.

¹⁹ Jylha (2018, p. 1292) lists the following motives for the Fed to change margin requirements, authorized in the Securities Exchange Act of 1934: "changes in stock market credit, changes in the market prices of stocks, changes in speculative activity, or overall inflationary pressure." For additional details on margin regulation, see Jylha (2018).

unique opportunity to study how leverage constraints affect the pricing of risk. We also control for these macroeconomic conditions in our analysis.

III.B. Data on Factor Hedge Portfolio Returns, Descriptive Statistics, and Control Variables

All variables are defined in Table II. Our analysis extends prior work to include the multiple factors from the models of Fama and French (1993, 1994, and 1996) and Carhart (1997). We note that several other multifactor models have emerged in recent years.²⁰ We opt to focus on the Fama and French three-factor and Carhart four-factor models for two reasons. First, our sample period covers the middle of the 20th century, when reliable data are unavailable for factors based on investment and profitability. For example, during this period, Carey (1969) emphasizes the lack of uniformity in the accounting treatment of total assets and expenses, which are required for constructing the investment and profitability factors. Second, Linnainmaa and Roberts (2018) do not find a return premium for investment and profitability before 1963. Similarly, Wahal (2018) finds no premium for investment over this earlier period, while finding some evidence of a profitability premium. Since dependable data are unavailable for these two factors since 1934, and they do not display priced risk or return predictability before 1963, they are unlikely to be helpful in explaining the cross section of stock returns over our sample period.

Data on risk factors are obtained from Kenneth French's library, and stock return data are from CRSP. We construct the factor hedge portfolio composed of high minus low beta stocks (MBeta) from the set of all NYSE stocks with price greater than \$5. We begin by estimating the beta of individual stocks every month (t), with a rolling window regression of the stock's excess return on the value-weighted CRSP market index over the prior 36 months, $t-36$ to $t-1$. The

²⁰ For example, consider the q-factor model of Hou, Xue, and Zhang (2015), the q5 model of Hou, Mo, Xue, and Zhang (2018), and the five and six-factor models of Fama and French (2015, 2018) and Barillas and Shanken (2018). In addition, Stambaugh and Yuan (2017) and Daniel, Hirshleifer, and Sun (2018) offer composite models based on risk and behavioral considerations, which are also effective in explaining the cross section of stock returns.

sample of stocks is then sorted each month (t) into deciles based on their estimated betas. The difference in future returns between the highest and lowest beta decile portfolios in month t represents the MBeta hedge portfolio return.

In Panel A of Table III, we provide summary statistics for the monthly returns on the three Fama and French factor portfolios and the MBeta portfolio. The mean monthly returns on these four factor hedge portfolios range from 20 to 70 basis points (bps) per month. Panel B provides summary statistics for the monthly time series of margin requirements, as well as the monthly intercept and slope coefficients for the SML analogues constructed from the three-factor and four-factor models.²¹ The mean (median) level of margin requirements over our sample period is 61% (65%), with a standard deviation of 15.7%. Similar to the CAPM case in Jylha (2018), the average monthly intercept estimated from the three-factor and four-factor models over this period is relatively large (i.e., 80 – 90 bps per month), while the average slope coefficient pertaining to the market factor is relatively small, at 20 – 30 bps. The mean monthly slopes of the SML analogues that pertain to the HML, and SMB range from 30 – 40 bps per month, and are close to their respective mean factor hedge portfolio returns in Panel A. In contrast, the slope of the SML analogue for the UMD factor (20 bps) is smaller than its mean return (of 70 bps).

The accounting variables required to calculate the book-to-market ratio are available from the Compustat annual database after 1950. Since Compustat data are not available prior to 1950, we use the historical book-to-market data from Kenneth French’s library for the earlier years in our sample, from 1934 to 1950.

²¹ In Section V below, we describe our construction of the intercepts and slopes of these SML analogues.

We account for the possible effects of prevailing macroeconomic and financial market conditions on our findings by including several controls. For example, we control for the supply of credit made available by brokers to investors, by collecting margin credit data from three separate sources for different overlapping periods.²² We use the percent change in margin credit over the previous twelve months, measured as the logarithm of the change in margin credit from month $t-13$ to $t-1$. We also control for the contemporaneous value-weighted excess market return in month t , and the lagged cumulative market returns over two recent periods, from month $t-12$ to $t-1$ and from month $t-36$ to month $t-13$. We further control for the volatility and skewness of daily market returns over month $t-12$ to $t-1$, and the value-weighted average aggregate daily turnover of all NYSE stocks from month $t-12$ to $t-1$. In addition, we obtain the price-to-dividend ratio for the S&P Composite Index from Robert Shiller's website, and we use the price-dividend ratio prevailing in month $t-1$.²³ We also control for other macroeconomic factors, including the percent change in the consumer price index (CPI), industrial production, and the money supply (M1) over the previous twelve months, measured as the change in the natural logarithm of each series from month $t-13$ to $t-1$. Data on the CPI, industrial production, and M1 are obtained from the Federal Reserve Bank of St. Louis' Fred database.²⁴

Finally, in our robustness tests we analyze the call spread, defined as the difference between the broker's call money rate and the three-month Treasury Bill rate. Call money rate data come from the Federal Reserve Board (1976a, Table 120) for the period 1934 to 1941, the Federal Reserve Board (1976b, Table 12.23) from 1942 to 1970, and the Survey of Current

²² We combine the following time-series: "Debit balances, Customers' debit balances (net)" from Table 143 of Federal Reserve Board (1976a) over the period between November 1931 and December 1937, "Customer credit, Net debit balances with NYSE firms secured by, U.S. Government securities, Other Securities" from Table 12.23 of Federal Reserve Board (1976b) over the period, January 1938 to December 1958, and "Margin debt" from the NYSE Facts and Figures database over the period, January 1959 to September 1975.

²³ <http://www.econ.yale.edu/~shiller/data.htm>.

²⁴ <https://fred.stlouisfed.org/>.

Business from 1971 to 1975.²⁵ Throughout the analysis, each control variable is standardized by subtracting its mean and dividing by its standard deviation over the past twelve months. The summary statistics for these controls are provided in Panel C of Table III.

IV. Margin Requirements and Returns to the Hedge Portfolio Associated with Each Factor

In this section, we directly investigate the two predictions from the theory of Black (1972) and Frazzini and Pedersen (2014) by analyzing the return dynamics of stocks with more or less risk in the months around changes in margin requirements. In particular, we estimate monthly time series regressions that examine the behavior of returns to the long and short legs of the four factor hedge portfolios, before or after these policy changes.

IV.A. Returns to the Factor Hedge Portfolios Before Changes in Margin Requirements

In this subsection, we examine the first prediction of this theory by estimating the following time series relation:

$$\begin{aligned}
 \text{Ret}_{k_t} = & \alpha + \beta_1 \text{Mgn_Increase}_{t+3_t} + \beta_2 \text{Mgn_Increase}_{t+2_t} + \beta_3 \text{Mgn_Increase}_{t+1_t} \\
 & + \beta_4 \text{Mgn_Decrease}_{t+3_t} + \beta_5 \text{Mgn_Decrease}_{t+2_t} + \beta_6 \text{Mgn_Decrease}_{t+1_t} \\
 & + \beta_7 \Delta \text{Mgn_Credit}_{t-1} + \beta_8 R_{m,t-12,t-1} + \beta_9 R_{m,t-36,t-13} + \beta_{10} \text{Volatility}_{m,t-12,t-1} \\
 & + \beta_{11} \text{Skewness}_{m,t-12,t-1} + \beta_{12} \text{Turnover}_{m,t-12,t-1} + \beta_{13} P/D_{m,t-1} + \beta_{14} \Delta \text{CPI}_{t-13,t-1} \\
 & + \beta_{15} \Delta M1_{t-13,t-1} + \beta_{16} \Delta IP_{t-13,t-1} + \varepsilon_t.
 \end{aligned} \tag{1}$$

where Ret_{k_t} = return in month t on each factor hedge portfolio ($k = \text{MBeta, HML, SMB, or UMD}$), as well as the long and short legs of each hedge portfolio;

$\text{Mgn_Increase}_{t+m_t}$ = Dummy variable that equals 1 if there is a future *increase* in margin requirements in month $t+m$, where $m = 1, 2, \text{ or } 3$, or zero otherwise;

$\text{Mgn_Decrease}_{t+m_t}$ = Dummy variable that equals 1 if there is a future *decrease* in margin requirements in month $t+m$, where $m = 1, 2, \text{ or } 3$, or zero otherwise;

²⁵ The survey is available at <http://www.bea.gov/scb/>.

and the other control variables are defined in Table II.

The results are provided in Table IV. Consider the coefficients of the six dummy variables in the top half of Table IV, which reveal whether the return on each factor portfolio in month t rises (or drops) *prior to* increases (or decreases) in margin requirements over the next three months ($t+1$, $t+2$, or $t+3$). Consistent with the first prediction and the evidence in Figure 1, the return in month t on the first three factors (MBeta, HML, and SMB) reveals a *positive* relation with anticipated future changes in margin requirements over the following three months. That is, these three hedge portfolio returns rise in the months *before* an increase in margin requirements and drop *before* a decrease in margin requirements. Moreover, these return dynamics are driven by significant changes in returns on the riskier stocks in the long leg of each factor portfolio (i.e., high beta, value, and small stocks) *prior to* the change in margin requirements. In contrast, the long and short legs of the momentum hedge portfolio behave similarly to each other in the months before increases or decreases in margin requirements. As a result, returns to the UMD hedge portfolio itself are largely unrelated to future margin changes.

In the bottom half of Table IV, the coefficients of the control variables generally have the expected signs when significant. For example, the monthly returns on most portfolios are inversely related to changes in the supply of margin credit, the price dividend ratio, and inflation.

Together, the evidence in Table IV supports the first prediction, indicating that investors bid up (or down) the more risky stocks in the long legs of the first three factor hedge portfolios prior to increases (or decreases) in margin requirements, relative to the less risky stocks in the short legs. In contrast, these results suggest that investors do not similarly rely on the momentum factor to adjust their risk exposure in anticipation of future changes in leverage constraints.

IV.B. Returns to the Factor Hedge Portfolios After Changes in Margin Requirements

In this subsection, we examine the second prediction of the theory of Black (1972) and Frazzini and Pedersen (2014) by estimating time series regressions that relate current or future returns on the factor portfolios to lagged margin requirements and the set of control variables.

IV.B.1. Lagged Margin Requirements and One-Month-Ahead (Current) Returns

We begin by relating the current portfolio return in month t associated with each factor to lagged margin requirements in month $t-1$, the contemporaneous excess market return, and the other controls, as follows:

$$\begin{aligned}
 \text{Ret}_{k_t} = & \alpha + \beta_1 \text{Margin}_{t-1} + \beta_2 (R_{m,t} - R_{f,t}) + \beta_3 \Delta \text{Mgn_Credit}_{t-1} + \beta_4 R_{m,t-12,t-1} \\
 & + \beta_5 R_{m,t-36,t-13} + \beta_6 \text{Volatility}_{m,t-12,t-1} + \beta_7 \text{Skewness}_{m,t-12,t-1} \\
 & + \beta_8 \text{Turnover}_{m,t-12,t-1} + \beta_9 P/D_{m,t-1} + \beta_{10} \Delta \text{CPI}_{t-13,t-1} + \beta_{11} \Delta \text{M1}_{t-13,t-1} \\
 & + \beta_{12} \Delta \text{IP}_{t-13,t-1} + \varepsilon_t.
 \end{aligned} \tag{2}$$

In Table V, we provide the coefficient of lagged margin requirements from this regression analysis for the four factor hedge portfolios (MBeta, HML, SMB, and UMD), as well as the long and short legs of each portfolio. The coefficients of the other control variables are generally similar to those provided in Table IV and are omitted here for brevity.

First, consider the top row of Table V, which provides the coefficient of lagged margin requirements from estimating Equation (2) for the MBeta, HML, SMB, and UMD hedge portfolios, respectively. Consistent with the second prediction and the evidence in Figure 1 and Table IV, the results indicate a significant negative relation between lagged margin requirements and subsequent one-month-ahead returns to hedge portfolios based on the first three factors (MBeta, HML, and SMB). That is, following an increase in margin requirements in month $t-1$, returns to the first three hedge portfolios are significantly lower in the following month. In contrast, returns to momentum (UMD) are unrelated to lagged margin requirements.

To understand the economic impact of this top row in Table V, consider the magnitudes of the changes in margin requirements during our sample period. Table I indicates that margin requirements were changed by +/- 10% seven times, by 15% 3 times, 20% six times, and 25% six times. In column (1) of Table V, the coefficient of lagged margin requirements is -0.05 (t-value = 3.26). This result implies that a 25% increase in margin requirements in month $t-1$ would be associated with a decline in the return on the MBeta hedge portfolio of 1.25% ($= -0.05 \cdot .25$) in the following month. For the HML or SMB factor in column (2) or (3) of Table V, the analogous coefficient of lagged margin requirements is -0.04 or -0.02 (t-value = -3.81 or -2.19), and the implied economic impact is a decline in the hedge portfolio return of 1.00% or 0.50% in the following month, respectively. In contrast, the coefficient of lagged margin requirements for UMD is 0.00 (t-value = 0.29). These results corroborate our preliminary findings in Figure 1, indicating that an increase (or decrease) in margin requirements in month $t-1$ is followed by a subsequent decline (or rise) in hedge portfolio returns based on the first three factors (MBeta, HML, and SMB), during the following month t . However, future returns to the momentum hedge portfolio are unaffected by changes in margin requirements.

Next we separately examine the long or short leg of each factor hedge portfolio. That is, we separately analyze high versus low beta stocks, value versus growth stocks, small versus big stocks, and winners versus losers. This separate analysis enables the data to distinguish between two potential alternative explanations for the negative relation we find in the top row of Table V – one that involves more risk-taking versus another that involves less mispricing.

On the one hand, consistent with Frazzini and Pedersen (2014) and Jylha (2018), higher margin requirements may prompt investors to take more risk by overweighting high beta stocks, value stocks, or small stocks, leading to overvaluation of these riskier groups of assets. In this

scenario, an increase in margin requirements should have a stronger negative effect on the future returns to these subsets of *riskier assets in the long legs* of the first three factor hedge portfolios.

On the other hand, higher margin requirements may instead limit the capital available to noise traders, making them less prone to buy the *overpriced assets in the short legs* of the HML and SMB factor portfolios (i.e., growth stocks and large stocks). In this case, an increase in margin requirements would mainly reduce the purchasing power of noise traders, and thereby decrease the overvaluation they cause in the short legs of the HML and SMB hedge portfolios.²⁶

The results for the long and short legs of each factor portfolio appear in the second and third rows of Table V. For the first three factors (MBeta, HML, and SMB), the negative relation between margin requirements and future returns is concentrated among the *riskier assets in the long leg* of each hedge portfolio (i.e., high beta, value, and small stocks). The F-tests at the bottom of the first three columns in Table V verify that the differential effect of lagged margin requirements on one-month-ahead returns is significantly stronger for the riskier stocks in the long leg of these three factor portfolios. Together, this evidence is more consistent with a risk-based explanation for the negative relation between margin requirements and future returns on these three factor hedge portfolios. In contrast, this evidence does not support the alternative explanation based on reduced overpricing in the short leg, which would result from less buying by noise traders given higher margin requirements.

Finally, the evidence for momentum deviates from that for the other three factors. In particular, while the fourth column of Table V reveals a significant negative relation between lagged margin requirements and subsequent returns on each leg of the momentum factor (UMD),

²⁶ Since individual investors rarely sell short, higher margin requirements should mainly curtail the *buying* of noise traders, if it limits their trading at all (Barber and Odean, 2008, and Odean, 1999). In Section IV.B.2 below, we discuss an alternative scenario in which higher margin requirements may limit the capital available to arbitrageurs.

this negative relation is similar in magnitude for winners and losers. Indeed, the F-test at the bottom of column (4) indicates no significant difference between these coefficients for the long leg versus the short leg. As a result, there is no significant relation between margin requirements and future returns to the combined UMD hedge portfolio itself.

IV.B.2. Lagged Margin Requirements and Longer-Term Future Returns

In this section, we consider another potential alternative explanation for our findings that returns to the first three factor hedge portfolios are significantly lower in the short run, following an increase in margin requirements. According to this alternative explanation, higher margin requirements may limit the capital available to arbitrageurs, which prevents them from correcting the mispricing or even allows noise traders to temporarily exacerbate this mispricing (e.g., see Campbell and Kyle, 1993, and De Long, Shleifer, Summers, and Waldman, 1990). If the prices of stocks in the long and short legs of the factor portfolios deviate further from fundamentals in the short run after an increase in margin requirements, for this reason, this deviation could lead to negative returns for the factor hedge portfolios that is not corrected by arbitrageurs.

We note that this alternative explanation is not consistent with our evidence of higher (lower) hedge portfolio returns for MBeta, HML, and SMB *prior to* future increases (decreases) in margin requirements. Furthermore, an additional implication of this alternative explanation is that, in the longer run after an increase in margin requirements, prices should ultimately converge back toward fundamentals, so that we should eventually observe a reversal from a negative relation to a positive relation. We test this additional implication by examining the relation between margin requirements and longer run future returns on each factor, for up to twenty-four months following the change in margin requirements in month $t-1$. This analysis requires calculating longer run future returns to the same set of stocks in each leg of the factor

hedge portfolios constructed in month t . However, the factors in Kenneth French's data library (HML, SMB, and UMD) are updated only annually, and the underlying stocks are unknown to us. Thus, it is not possible to calculate future returns on a monthly basis over longer horizons, for the same set of stocks in each Fama-French factor.

We overcome this problem by constructing our own replicating hedge portfolios each month for the HML, SMB, and UMD factors. These replicating portfolios are necessary for our analysis of longer-term future returns for the portfolios of stocks in each factor portfolio, as well as the long and short legs of each hedge portfolio, around changes in margin requirements. We follow Davis, Fama, and French (2000) to calculate the replicating portfolios for the HML and SMB factors. In particular, we use sorts based on the book to market data provided on Kenneth French's website to construct our own replicating portfolio for the HML factor, and we use the firm's market capitalization to construct our own SMB factor. We create the replicating hedge portfolio for momentum by ranking stocks each month (t) into deciles based on their cumulative stock returns over the prior twelve months, $t-13$ to $t-2$. We then form the UMD hedge portfolio that is long past winners (highest decile) and short past losers (lowest decile) in month $t-1$, and we compute the future return to this UMD portfolio for the next twenty-four months, t to $t+23$.

We begin by examining whether our replicating factor portfolios display similar behavior to the three Fama and French (1993) factors from Kenneth French's web site. The correlations between the monthly returns on our three replicating portfolios and the associated Fama and French factors (HML, SMB, and UMD) are 0.93, 0.87, and 0.85, respectively. This outcome suggests that we can extend inferences from our own replicating factor portfolios to the factor portfolios of Fama and French.

We next relate the longer run future returns on these replicating factor hedge portfolios to lagged margin requirements, as follows:

$$\text{Ret}_{k_{t+i, t+j}} = \alpha + \beta_1 \text{Margin}_{t-1} + \text{Controls} + \varepsilon_t. \quad (3)$$

Now the dependent variable is the longer run future return to each replicating factor hedge portfolio, as described above ($k = \text{MBeta}, \text{HML}, \text{SMB}, \text{or UMD}$). First, as before, we hold every replicating hedge portfolio for one month (t) following the change in margin requirements in month $t-1$. In addition, we hold each hedge portfolio over a series of future three-month periods that span the next twenty-four months, from month t to $t+2$, $t+3$ to $t+5$, $t+6$ to $t+8$, $t+9$ to $t+11$, $t+12$ to $t+14$, $t+15$ to $t+17$, $t+18$ to $t+20$, and $t+21$ to $t+23$. The resulting hedge portfolio return for every future three-month period ($\text{Ret}_{k_{t+i, t+j}}$) is then regressed on lagged margin requirements in month $t-1$ and the controls from Equation (2), which are defined in Table II.

In Panel A of Table VI, we provide the results of estimating Equation (2) and Equation (3) for the MBeta hedge portfolio. In Panels B, C, and D, we present the analogous evidence for HML, SMB and UMD, respectively. As expected, column (1) of each Panel reveals that the results for short run (one-month-ahead) future returns to all four replicating factor hedge portfolios are similar to the analogous evidence for the original Fama and French portfolios, provided in Table V above.

Next, we turn to the evidence for longer run future hedge portfolio returns in columns (2) to (9) of Table VI. This evidence indicates that the significant negative relation between lagged margin requirements and one-month-ahead returns for the first three factor portfolios (MBeta, HML, and SMB), in column (1), continues to prevail over each successive three-month period that spans the following 12 to 21 months, before becoming insignificant near the end of this 24-month period. Once again, the evidence for momentum deviates from the other three factors in

Table VI, since the longer-term future returns to momentum (UMD) are never significantly negatively related to past margin requirements throughout the next 24 months.

It is important to emphasize that, for the first three factor portfolios, there is no eventual reversal of this short run negative relation to a longer-term positive relation between margin requirements and future returns. This outcome does not support the alternative explanation based on a temporary divergence of prices further from fundamentals, due to limited capital available to arbitrageurs. Instead this evidence is more consistent with the second prediction from the theory of Black (1972) and Frazzini and Pedersen (2014).

V. Margin Requirements and the SML Analogues from Multifactor Models

In this section we examine the association between margin requirements and time series variation in the monthly intercept and slope coefficients of the SML analogues implied by the Fama-French (1993) three-factor model or the Carhart (1997) four-factor model. We measure this association using a two-stage analysis. In the first stage, each month (t) we begin by estimating the sensitivity of returns on a set of test assets to every factor over the previous 36 months. We then estimate the cross-sectional relation between the returns on these test assets and their respective estimated factor sensitivities in month t , to obtain the monthly intercept and slopes of the SML analogues for all factors. In the second stage, we estimate the time series relation between each monthly intercept or slope coefficient and lagged margin requirements, along with our set of control variables. We next discuss each stage of this analysis, in turn.

V.A. First Stage: Estimating Factor Sensitivities and the Intercept and Slopes of SML Analogues

In our first stage, we follow Cohen, Polk, and Vuolteenaho (2005) and Jylha (2018), who estimate the intercept and slope of the CAPM security market line. In Jylha (2018), stocks are first grouped each month (t) into twenty value-weighted portfolios based on their historical betas,

estimated with rolling regressions of excess stock returns on excess market returns over the previous 36 months. Next, each month (t) the value-weighted returns of each portfolio are regressed on excess market returns (the first factor) over the prior 36 months to obtain its ex-ante beta. Then, each month (t) the cross section of realized returns on these twenty portfolios of test assets are regressed on their ex-ante betas. The resulting monthly intercept and slope of the CAPM security market line are retrieved from this last regression.

We employ similar methodology, with an expanded approach that enables us to obtain the monthly intercept and slopes for the SML analogues corresponding to all factors included in either the three-factor model or the four-factor model. We wish to analyze test assets that vary along all dimensions embodied in either multifactor model. We therefore begin by stratifying the set of all NYSE stocks each month (t) according to the three factors in the Fama and French (1993) model, or the four factors in the Carhart (1997) model, respectively, in order to generate portfolios of test assets that vary along each dimension analyzed.

Consider our analysis of the Fama and French (1993) three-factor model. Here we wish to analyze test assets that vary along the three dimensions: beta, book-to-market, and size. Thus, we independently sort stocks into four groups every month (t) based on each of the three dimensions: (i) the stock's historical market beta estimated over months $t-36$ to $t-1$, (ii) book-to-market ratio for the prior fiscal year, and (iii) firm size in month $t-1$. This $4 \times 4 \times 4$ sorting scheme generates a set of 64 portfolios of test assets each month (t), stratified along all three dimensions. The value-weighted returns for each portfolio of test assets are then regressed on each of the three factors over the previous 36 months ($t-36$ to $t-1$), to retrieve the ex-ante sensitivity of each portfolio's return to the market, HML, and SMB factors, respectively. Finally, the cross section of value-weighted excess returns to these 64 portfolios in month t are regressed

on their three ex-ante sensitivities estimated above. This last regression yields the monthly intercept and slope coefficients for the SML analogues implied by the three-factor model.²⁷

V.B. Second Stage: Relating Intercepts and Slopes of SML Analogues to Margin Requirements

In the second stage, we regress the monthly intercept or each slope coefficient from the SML analogues against lagged margin requirements and the controls defined above, as follows:

$$\text{Intercept}_t = \alpha_1 + \beta_1 \text{Margin}_{t-1} + \text{Controls} + \varepsilon_{1t}, \quad (4)$$

$$\text{Slope}_k_t = \alpha_2 + \beta_2 \text{Margin}_{t-1} + \text{Controls} + \varepsilon_{2t}, \quad (5)$$

where Intercept is the intercept, and Slope_k is the slope coefficient for the SML analogue associated with each factor estimated in month t , implied by the three-factor or four-factor model (i.e., k = the market return, HML, SMB, or UMD). All variables are defined in Table II.

In Table VII, we present the results for each second stage regression estimated. Columns (1) to (4) in Panel A present the analysis for the monthly time series regressions based on the intercept and slope coefficients from the three-factor model (including the market, HML, and SMB). Columns (1) to (5) in Panel B present the analogous results for the four-factor model (including the market, HML, SMB, and UMD). Robust t-ratios are provided in parentheses.

In Panels A and B of Table VII, the monthly intercepts from the three-factor and four-factor models both reveal a significant positive relation with lagged margin requirements. This positive relation suggests that these multifactor models fail to adequately explain the variation in the performance of the test assets analyzed when margin requirements are varied. On the other

²⁷ Our analysis of the Carhart (1997) four-factor model is similar. Here, each month we independently sort NYSE stocks into three groups based on each of the four factors: (i) beta, (ii) book-to-market, (iii) size, and (iv) momentum returns over the past twelve months. This $3 \times 3 \times 3 \times 3$ sorting scheme generates 81 portfolios of test assets each month. The value-weighted returns to each of these 81 portfolios are then regressed on each of the four factors over the prior 36 months, to retrieve the 81 sensitivities to each of these four factors. Finally, the cross section of value-weighted excess returns to these 81 portfolios in month t are regressed on their four ex-ante sensitivities estimated above, to get the monthly intercept and slope coefficients of the SML analogues implied by the four-factor model.

hand, the slope coefficients for the first three factors (i.e., the market, HML, and SMB) are negatively related to margin requirements. This evidence is consistent with the second prediction of Black (1972) and Frazzini and Pedersen (2014), indicating that tighter leverage constraints result in flatter SML analogues for the market, HML, and SMB factors, which implies lower subsequent compensation for these aspects of risk. In contrast, there is no significant relation between margin requirements and the slope of the fourth momentum factor (UMD) in Panel B.

To understand the economic significance of these results, consider the implications of a 25% change in margin requirements for the intercept or slope coefficient that pertains to each factor. For example, in columns (1) to (4) of Panel A in Table VII, the coefficient of lagged margin requirements is 0.02 (t-ratio = 1.8) for the regression involving the intercept, and is -0.03 (with t-ratios that range from -2.5 to -3.2) for the regressions involving the three factors (i.e., the market, HML, and SMB). This evidence indicates that a 25% increase in margin requirements in month t would be associated with an average increase in the alpha of the three-factor model in month $t+1$ by 50 basis points (i.e., 0.02×0.25), and an average decline in the slope of each SML analogue by 75 basis points (i.e., -0.03×0.25).

VI. Extensions and Robustness Tests

In this section, we examine the robustness of our main results when we analyze alternative test assets or consider additional control variables.

VI.A. Alternative Test Assets

In this subsection, we repeat the analysis from Table VII using two alternative sets of test assets. We generate the first set of alternative test assets by conducting a two-way 5×5 sorting scheme each month (t), in which we independently partition the set of all NYSE stocks into five groups based on just the two firm attributes, book-to-market and size, to form 25 value-weighted

portfolios. Our second alternative set of test assets includes the Fama and French 49 industry portfolios each month (t), which are available from the Kenneth French data library. In the latter analysis, we exclude the eight industries that have missing observations sometime during our sample period, which leaves 41 industries with a complete return history.²⁸

For each alternative set of test assets, we follow the same two-stage regression analysis to retrieve the monthly intercept and slopes of the SML analogues for each factor, and then estimate the relation between lagged margin requirements and each intercept or slope coefficient. In Panel A (B) of Table VIII, we provide the results from estimating Equation (4) and Equation (5) using the first (second) alternative set of test assets. In columns (1) to (4) of each Panel, we present the results for the intercept and SML slope coefficients based on the three-factor model. In columns (5) to (9), we provide the analogous results for the four-factor model.

The results in both Panels of Table VIII are similar to the evidence in Table VII. In particular, the monthly intercept from each multifactor model is again positively related to margin requirements, while the SML slope coefficients for the first three factors (i.e., the market, HML, and SMB) are negatively related to margin requirements. In contrast, the slope of the fourth momentum factor (UMD) is unrelated to margin requirements. This analysis shows that our main results for Equation (4) and Equation (5) are robust when we base the analysis on alternative test assets each month.

VI.B. Market Neutral Factor Portfolios

Our explanation for the negative relations between lagged margin requirements and the slope coefficients for the SML analogues pertaining to the HML and SMB factors implies that

²⁸ Results are robust when we exclude just the missing observations each month (t), instead of excluding all observations from the eight industries that have some missing observations. Results are also robust when we analyze the Fama and French 30 or 48 industry portfolios.

these two hedge portfolios capture aspects of risk that differ from the market beta. However, Liu (2018) notes that the hedge portfolio returns associated with many asset pricing anomalies reveal a negative sensitivity to the market portfolio (i.e., they have a negative market beta). As a result, hedge portfolio returns associated with many anomaly variables mechanically incorporate the betting-against-beta anomaly of Frazzini and Pedersen (2014). According to Liu (2018), it is the betting-against-beta anomaly that drives the returns to many anomalies, rather than any true anomalous predictive relation associated with those anomaly variables.

While Liu (2018) does not examine the book-to-market and firm size anomalies that are associated with HML and SMB in our analysis, we find that the correlations of Mbeta with HML and SMB are significantly positive (at 0.40 and 0.66, respectively).²⁹ These high correlations may reflect a tendency for value stocks and small stocks to have higher market betas, making our analysis susceptible to a critique similar to that in Liu (2018). That is, this high correlation suggests that our results may be driven by a failure to control for the influence of market beta on HML and SMB, rather than by investors' response to more binding leverage constraints.

We address this issue by constructing new replicating portfolios for HML, SMB, and UMD that are neutral with respect to the market (i.e., that have zero market betas), and repeating our main analysis using these market-neutral factor portfolios. We construct these market-neutral factor portfolios using a methodology similar to Liu (2018) by eliminating high (low) beta stocks from the long (short) legs of the HML and SMB factors, respectively. For example, for the HML factor we eliminate high beta stocks from the value portfolio and low beta stocks from the growth portfolio. In particular, we examine a subset of the value stock portfolio (the long leg of HML), by retaining only stocks that are below the 70th percentile in terms of their market beta,

²⁹ In contrast, the correlation between MBeta and UMD is -0.37.

and higher than the 70th percentile in terms of their book-to-market ratio. Similarly, we retain a subset of the growth stock portfolio (the short leg of HML) that are above the 30th percentile in terms of their market beta, and below the 30th percentile in terms of their book-to-market ratio. We follow a similar approach for the long and short legs of the SMB and UMD factors.³⁰

The correlation between MBeta and our market-neutral factor portfolios (labeled N-HML, N-SMB, and N-UMD) are 0.03, -0.018, -0.206, respectively. Hence, this method yields N-HML and N-SMB portfolios that are indeed market-neutral, since they have zero correlation with the MBeta portfolio. In addition, this method produces a portfolio for momentum (N-UMD) that has a smaller negative correlation with the MBeta portfolio.

Next, we repeat our analyses from Table V and Table VII using these market-neutral portfolios, N-HML, N-SMB, and N-UMD. The evidence for future one-month-ahead returns to these market-neutral hedge portfolios is presented in Panel A of Table IX, while the evidence for the intercepts and slopes of the SML analogues for the three- and four-factor models appears in Panel B. The main results and conclusions are unchanged. In Panel A, lagged margin requirements are negatively related to subsequent returns on the market-neutral factor portfolios, N-HML and N-SMB, while they are unrelated to future returns on the market-neutral N-UMD factor portfolio.³¹ Similarly, in Panel B, margin requirements are once again positively related to the intercept and negatively related to the slopes of the first two market-neutral factors, N-HML and N-SMB, while they are unrelated to the slope of the N-UMD factor. We conclude that our

³⁰ Since UMD has a negative correlation with MBeta, we eliminate low (high) beta stocks from the long (short) legs of the UMD factor.

³¹ In untabulated results, we find that the negative relation between margin requirements and one-month-ahead returns to the first two market neutral factor portfolios, N-HML and N-SMB, documented in Table IX, also extends further into the future when we examine longer term future returns, similar to the results in Table VI.

results are robust when we control for the sensitivity of the HML, SMB, and UMD factors to market beta, and therefore our conclusions are not subject to the critique of Liu (2018).

VI.C. Controlling for the Cost of Leverage for Investors

In this subsection, we repeat the analysis from Tables V and VII, but we also control for investors' cost of leverage. When lending and borrowing rates differ, efficient portfolios that involve borrowing lie on a flatter line than the alternative set of efficient portfolios that involve lending. Thus, in addition to restrictions on borrowing, another potential market friction that could lead to a flatter relation between expected returns and return sensitivities (i.e., a flatter SML analogue) for various risk factors is the difference between borrowing and lending rates.

Here we expand Equations (2), (4), and (5) to include a proxy for the difference between borrowing and lending rates, or investors' cost of leverage. Our proxy is the call spread, defined as the difference between the broker's call money rate and the three-month Treasury Bill rate. Theoretically, a higher call spread could be associated with a flatter SML analogue for each factor. As a result, the call spread may be positively related to the intercept and negatively related to the slope coefficient for each factor.³²

In Table X, we present this expanded analysis of Equations (2), (4) and (5). For every regression, we present the evidence for two specifications that include the lagged call spread, with and without lagged margin requirements. For brevity, we only present the coefficients for our two main variables of interest, lagged margin requirements and the call spread.

In Panels A and B of Table X, we estimate the expanded version of Equation (2), to analyze *returns* on the long leg and the short leg of each factor portfolio, as well as the hedge portfolio itself. In Panel A we provide the results for MBeta and HML, while Panel B presents the

³² See Cohen, Polk, and Vuolteenaho (2005), Jylha (2018), and Statman (1987).

results for SMB and UMD. Similar to the evidence in Table V, the results indicate a significant negative relation between lagged margin requirements and the monthly return to the first three factors, which is driven by the riskier stocks in the long leg of each factor hedge portfolio. In contrast, lagged margin requirements are again unrelated to returns on momentum (UMD).

In Panels C and D of Table X, we present the analogous results from estimating a similarly expanded version of Equation (4) and Equation (5) in the second stage of our analysis of the *SML intercept and slope coefficients*. In Panel C, we provide the results for the Fama and French (1993) three-factor model, and in Panel D we present the results for the Carhart (1997) four-factor model. Once again, including the lagged call spread in the model does not alter the coefficient of lagged margin requirements from Table VII, which remains significantly positive in regressions involving the intercept, and significantly negative in regressions involving the first three factors of each model (i.e., the market, HML, and SMB). In contrast, there is again no significant relation between lagged margin requirements and the SML slope analogue for the momentum factor (UMD).

Throughout all specifications in Panels A – D of Table X, the coefficient of the lagged call spread is never significantly different from zero. Furthermore, this coefficient does not change substantially when we add lagged margin requirements to the model. This evidence indicates that our results from Tables V and VII are not driven by investors' cost of leverage, or by some unspecified association between margin requirements and this cost of leverage.

VI.D. Disagreement, Short Sale Constraints, and Margin Requirements

Hong and Sraer (2016) examine the influence of investor disagreement and short sale constraints on the slope of the CAPM security market line. They argue that, when investors disagree about prospects for the macroeconomy, assets with a high market beta are more

sensitive to this disagreement and thus experience greater divergence of opinions about their future payoffs. Because of short selling restrictions, these high beta stocks may tend to be held more by optimists and thus become overvalued. Consequently, in the presence of high aggregate disagreement and short selling constraints, the lower expected returns for overpriced stocks with a high market beta could make the SML flatter, or even downward sloping. In contrast, when aggregate disagreement is low, the security market line should have its normal upward slope. Hong and Sraer (2016) find that the CAPM security market line is indeed flatter when investor disagreement is high, consistent with their theory.

In this subsection, we investigate whether our main results may be driven by elevated investor optimism embedded in stocks with a high market beta, in the presence of high aggregate disagreement and short selling constraints, rather than by the leverage channel we propose. We further note that, in addition to the market factor, the HML and SMB factors may also capture different aspects of investor behavior that are sensitive to dispersion of opinions about future payoffs. For example, during periods of high disagreement, stocks with high sensitivity to HML and SMB (e.g., value stocks and small stocks) might also tend to be held by more optimistic investors, which could push up their prices and lower their expected returns. Hence, our findings for the HML and SMB factors may also conceivably be explained by investor disagreement and short selling constraints rather than by the channel involving leverage constraints.

We investigate this issue by repeating the analysis in Tables V and VII, but expanding Equations (2), (4), and (5) to include various proxies for market-wide investor disagreement or aggregate short selling activity, as well as their interaction with margin requirements. Specifically, we analyze the following three measures of aggregate disagreement in month t : (i) value-weighted average idiosyncratic volatility across all stocks, (ii) aggregate value-weighted

share turnover, and (iii) the cross-sectional standard deviation of monthly stock returns. In addition, we consider the aggregate short interest ratio as a measure of total short selling activity.

We create four dummy variables to capture periods of high aggregate disagreement or short selling activity, which are assigned a value of one if each respective measure is above the median during our sample period, and zero otherwise. When we analyze factor returns in Equation (2), if our results are driven by high market-wide disagreement or low short selling activity, rather than by changes in margin requirements, the coefficients of these dummy variables should be significant when added to Equations (4) and (5), while the coefficient of lagged margin requirements should be attenuated. When we analyze the SML intercepts and slopes in Equations (4) and (5), if high market-wide disagreement results in a flatter SML analogue for each factor due to short selling constraints, the coefficient of the interaction between margin requirements and the first three disagreement dummy variables should be positive in the time series regressions involving the monthly intercept, and negative for those involving the monthly SML slope for each factor. Alternatively, during periods of low aggregate short selling activity (perhaps due to short selling constraints), negative views are less likely to find their way into the marketplace. Since stocks with high risk sensitivities (e.g., high market beta, value, or small stocks) are more likely to be affected by high disagreement, they may become more overvalued when short selling constraints are more binding, leading to subsequent negative returns. In this case, the coefficient of the interaction between margin requirements and the short selling dummy would be negative for the analysis of the monthly intercept, and positive for the monthly SML slope coefficients.

In Table XI, we provide the results from estimating these expanded versions of Equations (2), (4), and (5). The evidence for future one-month-ahead returns on the factor portfolios in

Equation (2) is presented in Panels A and B of Table XI, while the evidence for the intercepts and slopes of the SML analogues for the three- and four-factor models from Equations (4) and (5) appears in Panels C and D. In Panels A and B, the coefficient of lagged margin requirements remains significantly negative for the first three factor portfolios (MBeta, HML, and SMB), and this negative relation is still driven by the riskier stocks in the long leg of each hedge portfolio. In Panels C and D, the coefficient of lagged margin is once again generally positive and significant for regressions involving the intercept (Equation (4)), but negative and significant for regressions involving the slopes of the first three factors (Equation (5)).

In contrast, throughout all four Panels of Table XI, the interaction terms between lagged margin and the dummy variables for periods of high aggregate *Disagreement* or *Short Interest* are generally insignificant, and they have mixed signs across regressions involving the different specifications. We conclude that our main results in Tables V and VII are not driven by unusually high demand from optimistic investors during periods of high market-wide disagreement, or by short sale restrictions that prevent the aggregate negative views of short sellers from entering the marketplace.³³

VII. Conclusion

One fundamental premise of the theory of Black (1972) and Frazzini and Pedersen (2014) is that an impending increase (or decrease) in leverage constraints prompts investors to shift away from (or towards) their optimal portfolios, by buying (or selling) assets with more risk. We extend the emerging literature on this theory by testing two divergent predictions of this theory, regarding the initial versus subsequent return dynamics of stocks with more or less risk around

³³ We have also estimated expanded versions of Equations (2), (4) and (5) which include a triple interaction term that considers periods of: (a) high margin requirements, (b) high disagreement, and (c) high short selling activity. The coefficients for lagged margin requirements are also robust to these alternative specifications.

changes in margin requirements, in a multifactor setting. In particular, we analyze the asset pricing implications of risk-taking behavior associated with factors from the Fama and French (1993) three-factor model and the Carhart four-factor (1997) model, when margin requirements are changed. These multiple factors include HML, SMB, and UMD, along with a fourth hedge portfolio that is long stocks with a high market beta and short stocks with a low market beta (labeled MBeta).

Following Jylha (2018), we consider the Fed's 22 changes in margin requirements over the period, 1934 – 1974, as shocks that affected investors' access to leverage, which offer a unique opportunity to empirically analyze the predictions from this theory. First we examine the returns on these four factor portfolios, as well as the long and short legs of each hedge portfolio, before and after changes in margin requirements. Second we analyze how margin requirements affect the slopes of the security market line (SML) analogues pertaining to these factors, that are implied by the three-factor model and four-factor models.

Consistent with the fundamental premise of this theory, returns to the riskier stocks in the long legs of three factor hedge portfolios (i.e., high beta stocks, value stocks, and small stocks) initially rise (fall) in the months prior to increases (decreases) in margin requirements, and subsequently reverse after the policy change. In addition, lagged margin requirements are positively related to the intercept of the SML associated with the three-factor and four-factor models, but negatively related to the slopes of the SML analogues that pertain to the market, HML, and SMB factors. This evidence is consistent with a tendency for investors to overweight riskier high-beta stocks, value stocks, and small stocks when they face more binding leverage constraints. In contrast, margin requirements are unrelated to the analogous hedge portfolio returns or the slope of the SML analogue associated with the momentum factor (UMD).

Our results are robust when we incorporate additional controls for the cost of leverage, aggregate disagreement, and short sale constraints. They are also unchanged when we analyze long term future returns, or factors for book-to-market, size, and momentum that are constructed to be market-neutral. Furthermore, this evidence remains when we use alternative test assets to estimate the slopes of the SML analogues associated with the market, HML, SMB, and UMD.

This paper contributes to the asset pricing literature that encompasses the CAPM and multifactor models. Prior work documents that the security market line is too flat relative to the CAPM, and argues that leverage constraints play a role (e.g., Black, 1972, Brennan, 1971, Frazzini and Pedersen, 2014, Jylha, 2018, and Mehrling, 2005). We expand upon this prior work by showing that leverage constraints also have a bearing on the failure of multifactor models to adequately explain the cross section of expected returns. Therefore, future studies of multifactor models should consider the influence of leverage constraints, as well as other frictions that may affect the performance of these asset pricing models. Although our analysis of multifactor models is empirically motivated, our finding that leverage constraints affect the demand, and thus prices, for riskier stocks associated with these factors is also consistent with the demand-based equilibrium model of Kojien and Yogo (2019).

This paper also contributes to the broad literature on whether returns to various factors reflect compensation for risk or market mispricing. Our results suggest that investors rely on the market, SMB, and HML factors to adjust their risk exposure when leverage constraints become more or less binding. This analysis is consistent with the view that returns to these three factors reflect, at least partly, a premium for bearing risk. In contrast, our analysis does not support the view that investors rely on the momentum factor (UMD) to adjust their risk exposure when leverage constraints are changed.

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Appendix A. Wall Street Journal Quotes Anticipating Changes in Margin Requirements by the Federal Reserve

This Appendix provides several quotes from the *Wall Street Journal* which document that, during our sample period (October 1934 through September 1975), the Federal Reserve often announced (and the market responded to) its intention to change margin requirements well in advance.

Current margin level and the WSJ date: none, September 21, 1934

Next closest or recently required margin level and the decision date: 45%, October 1, 1934

News headline: “Margin Requirements Before Board”

Quote: “Federal Reserve regulations on credit extension by brokers, dealers, and bankers for security trading have been completed by the Federal Reserve Board members for final action. Officials of the board look for final action within the next day or two.”

Current margin level and the WSJ date: 55%, May 21, 1937

Next closest or recently required margin level and the decision date: 40%, October 27, 1937

News headline: “Margin Proposal”

Quote: “Representative Matthew T. Merritt (N. Y.) has introduced another bill in the House to amend Sub-section 1 of Section 7 of the Securities and Exchange Act of 1934 providing for a 35% margin requirement. Bill provides that Federal Reserve System requirements shall provide initial extension of credit on the basis of “65% of the current market price of the security.” A similar bill was introduced by Representative Merritt last month.”

Current margin level and the WSJ date: 50%, June 07, 1945

Next closest or recently required margin level and the decision date: 75%, July 3, 1945

News headline: “White House Backing Sought to Curb Real Estate, Stock Prices”

Quote: “The Federal Reserve Board has statutory authority to raise margin requirements on securities sales to 100%. This would put market transactions on a strictly cash basis. Reserve Board Chairman Eccles has hinted during the past few months that the Reserve Board will take such action, but he has also made it clear that removal of credit from market transactions would

have but limited effect. There is today only a limited amount of credit in the market. Also, 100% margins for stock transactions would have no effect on real estate.”

Current margin level and the WSJ date: 50%, August 05, 1958

Next closest or recently required margin level and decision date: 70%, August 4, 1958

News headline: “Borrowing Not Excessive, Funston Says; Brokers See Little Effect on Prices”

Quote: “Paine-Webber’s Mr. Kurtz thinks “shrewd people” will be buying in the wake of the requirements boost. A good deal of past week’s buying probably was in anticipation of this margin change, he noted.”

Current margin level and the WSJ date: 90%, May 19, 1960

Next closest or recently required margin level and the decision date: 70%, July 27, 1960

News headline: “Reserve Board Eager to Cut Stock Margin Requirement Below %90”

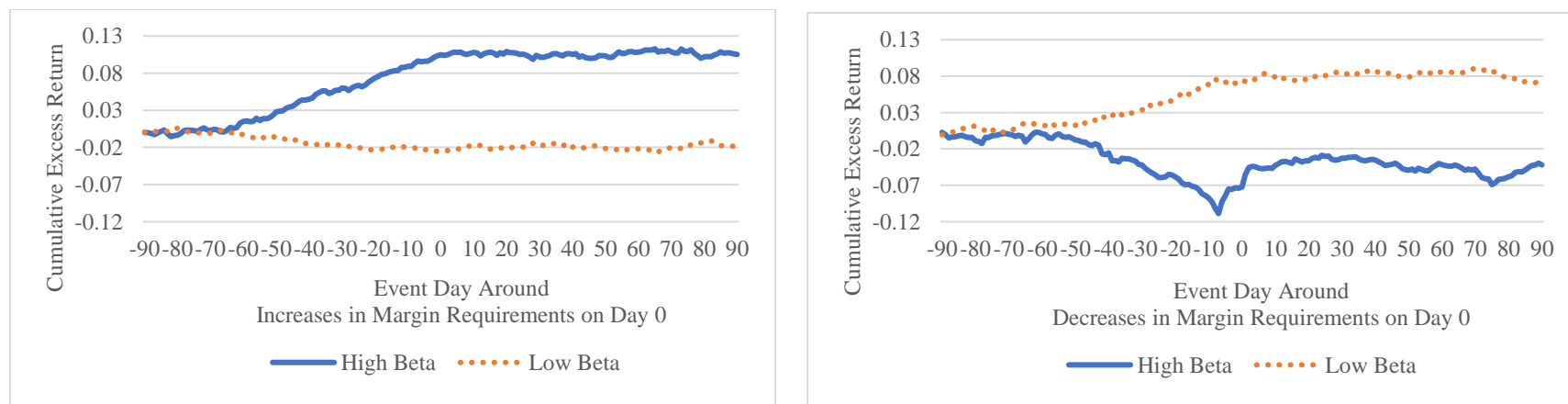
Quote: “The Federal Reserve is eager to cut the 90% stock margin requirement as soon as stock market prices stabilize for perhaps four or five days. If and when the cut comes-and the trend in stock prices will largely determine the timing-it probably will be deep, possibly to 70% and maybe even to 50%.

Federal Reserve officials have felt for some time that the present 90% margin, established in October 1958, to curb what then appeared to be a threat of excessive stock market speculation, is too high under present market conditions. The margin means investors must put up 90 cents cash or equivalent on each \$1 stock purchase and can borrow only 10 cents from a broker or a bank.”

Figure 1. Abnormal Returns to the Long and Short Legs of Factor Hedge Portfolios around Changes in Margin Requirements

Panels A – D of this Figure plot the mean abnormal returns to the long and short legs of the four factor hedge portfolios (MBeta, HML, SMB, and UMD), over the 181 days around the 12 increases or the 10 decreases in margin requirements during the period, Oct. 1934 – Sep. 1975. Abnormal returns are the differences between daily cumulative returns to each portfolio and the CRSP value-weighted market index, where cumulating begins on day -90. In each Panel, the solid line plots the long leg (i.e., high beta, value, small, or winner stocks) while the dotted line plots the short leg (i.e., low beta, growth, big, or loser stocks). The left side of each Panel plots the results around increases in margin requirements, while the right side plots the results for decreases in margin requirements (on day 0).

Panel A. Abnormal Returns for Long and Short Legs of MBeta Hedge Portfolio



Panel B. Abnormal Returns for Long and Short Legs of HML Hedge Portfolio

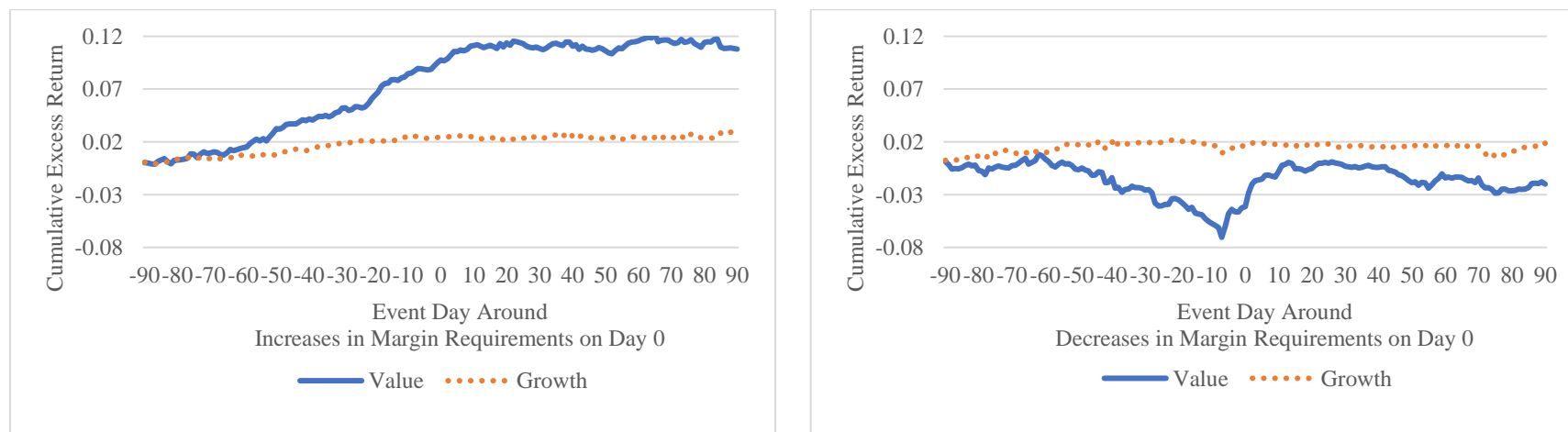
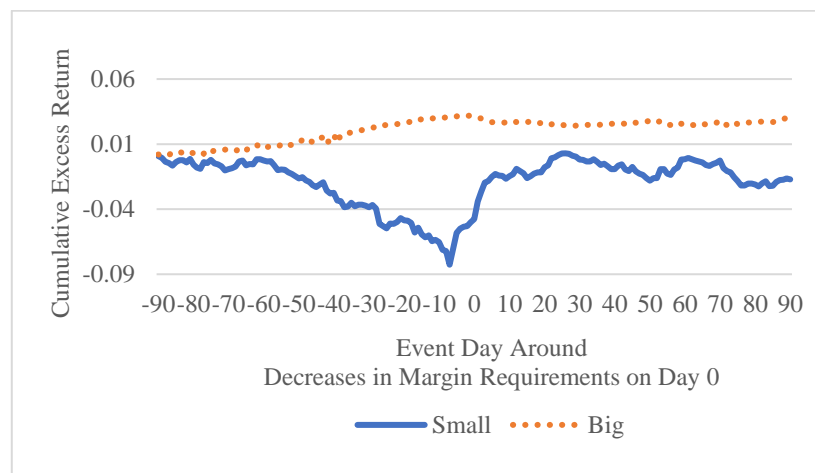
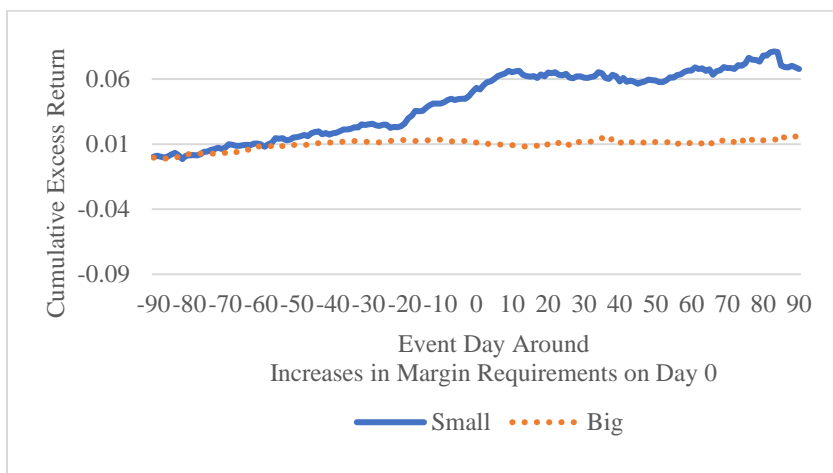


Figure 1, continued

Panel C. Abnormal Returns for Long and Short Legs of SMB Hedge Portfolio



Panel D. Abnormal Returns for Long and Short Legs of Momentum (UMD) Hedge Portfolio

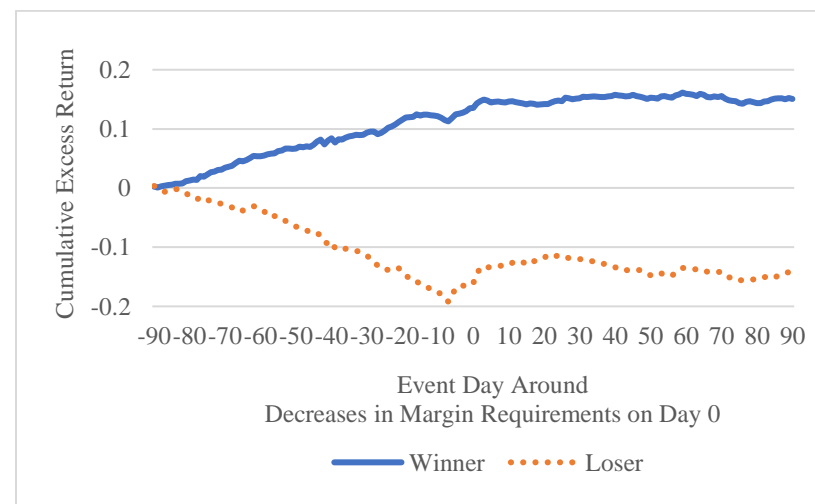
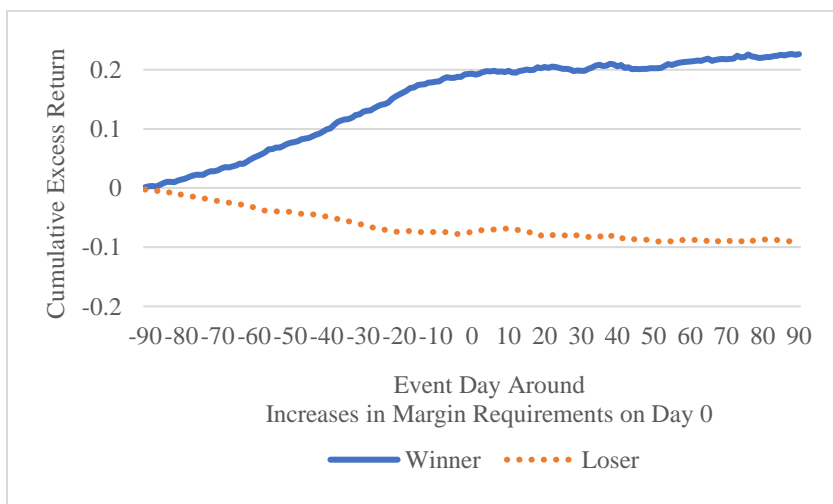


Table I. Changes in Margin Requirements

This table lists the dates of the Federal Reserve Board's changes in Regulation T minimum margin requirements over the period, October 1934 to January 1974, including the decision and effective dates. The decision date is when the Fed made the decision to change the margin requirement to the new level. The new requirement became effective on the effective date.

Decision Date (1)	Effective Date (2)	Change (3)	Level (4)
	October 1, 1934		45%
January 24, 1936	February 1, 1936	+10%	55%
October 27, 1937	November 1, 1937	-15%	40%
February 2, 1945	February 5, 1945	+10%	50%
July 3, 1945	July 5, 1945	+25%	75%
January 17, 1946	January 21, 1946	+25%	100%
January 17, 1947	February 1, 1947	-25%	75%
March 28, 1949	March 30, 1949	-25%	50%
January 16, 1951	January 17, 1951	+25%	75%
February 20, 1953	February 20, 1953	-25%	50%
January 4, 1955	January 4, 1955	+10%	60%
April 22, 1955	April 23, 1955	+10%	70%
January 15, 1958	January 16, 1958	-20%	50%
August 4, 1958	August 5, 1958	+20%	70%
October 15, 1958	October 16, 1958	+20%	90%
July 27, 1960	July 28, 1960	-20%	70%
July 9, 1962	July 10, 1962	-20%	50%
November 5, 1963	November 6, 1963	+20%	70%
June 7, 1968	June 8, 1968	+10%	80%
May 5, 1970	May 6, 1970	-15%	65%
December 3, 1971	December 6, 1971	-10%	55%
November 22, 1972	November 24, 1972	+10%	65%
January 2, 1974	January 3, 1974	-15%	50%

Table II. Variable Definitions

Factor Hedge Portfolios	
HML _t	Return on high minus low book-to-market hedge portfolio from Kenneth French's web site in month <i>t</i> .
SMB _t	Return on small minus big firm size portfolio from Kenneth French's web site.
UMD _t	Return on up minus down momentum portfolio from Kenneth French's web site.
MBeta _t	Return on high minus low beta hedge portfolio that is long the decile of stocks with a high market beta and short the decile with a low market beta in month <i>t</i> .
Dependent Variables	
Ret _{k,t} or Ret _{k,t,t+2} or Ret _{k,t+i,t+j}	The return in month <i>t</i> , or the cumulative return over successive three-month periods that span the next 24 months, from <i>t</i> to <i>t+2</i> , or from months <i>t+i</i> to <i>t+j</i> , for the hedge portfolio based on each factor (i.e., <i>k</i> = MBeta, HML, SMB, or UMD), as well as the long or short leg of each factor hedge portfolio.
Intercept _t or Slope _{k,t}	The intercept or slope coefficient for the security market line (SML) analogue associated with each factor estimated in month <i>t</i> (i.e., <i>k</i> = the market return, HML, SMB or UMD), implied by the three-factor or four-factor model.
Independent Variables	
Mgn_Increase _{t+m,t}	Dummy variable assigned a value of 1 if there is a future <i>increase</i> in margin requirements in month <i>t+m</i> , where <i>m</i> = 1, 2, or 3 months later, or zero otherwise.
Mgn_Decrease _{t+m,t}	Dummy variable assigned a value of 1 if there is a future <i>decrease</i> in margin requirements in month <i>t+m</i> , where <i>m</i> = 1, 2, or 3 months later, or zero otherwise.
Margin _{t-1}	The lagged value of Reg T margin requirements that were in effect during month <i>t-1</i> .
ΔMgn_Credit _{t-13,t-1}	Change in the natural log of aggregate margin credit in the U.S. from month <i>t-13</i> to <i>t-1</i> .
R _{mt} - R _{ft}	Excess value-weighted market return in month <i>t</i> .
R _{m,t-12,t-1}	Cumulative lagged value-weighted market return from month <i>t-12</i> to <i>t-1</i> .
R _{m,t-36,t-13}	Cumulative lagged value-weighted market return from month <i>t-36</i> to <i>t-13</i> .
Volatility _{m,t-12,t-1}	Standard deviation of daily stock market returns from month <i>t-12</i> to <i>t-1</i> .
Skewness _{m,t-12,t-1}	Skewness of daily stock market returns from month <i>t-12</i> to <i>t-1</i> .
Turnover _{m,t-12,t-1}	Average value-weighted aggregate market daily share turnover from month <i>t-12</i> to <i>t-1</i> .
P/D _{m,t-1}	The stock market price-dividend ratio measured at the end of month <i>t-1</i> .
ΔCPI _{t-13,t-1}	Change in the natural log of the CPI from month <i>t-13</i> to <i>t-1</i> .
ΔM1 _{t-13,t-1}	Change in the natural log of the money supply (M1) from month <i>t-13</i> to <i>t-1</i> .
ΔIP _{t-13,t-1}	Change in the natural log of industrial production from month <i>t-13</i> to <i>t-1</i> .
Call_Spread _t	Difference between broker's call money rate and 3-month Treasury Bill rate in month <i>t</i> .

Table III. Descriptive Statistics

Panel A of this table provides summary statistics for the time series of monthly returns on the three factors that are available from Kenneth French's web site (HML, SMB, and UMD) over the period from October 1934 to September 1975. This Panel also provides summary statistics for MBeta, the monthly return on our high-minus-low beta hedge portfolio that is long the decile of stocks with a high market beta and short the decile with a low market beta. Panel B provides descriptive statistics for the monthly time series of margin requirements instituted by the Federal Reserve, as well as the monthly intercept and slope coefficients that we construct from the SML analogues associated with the Fama-French (1993) three-factor and Carhart (1994) four-factor models, respectively. This latter analysis uses the set of test assets obtained from our $4 \times 4 \times 4$ sorting scheme along the three dimensions: beta, book-to-market, and size for the Fama-French (1993) three-factor model, and the $3 \times 3 \times 3 \times 3$ sorting scheme along the four dimensions: beta, book-to-market, size, and momentum for the Carhart (1993) four-factor model. Panel C presents summary statistics for the control variables.

Panel A. Descriptive Statistics for Returns on the Factor Hedge Portfolios

	MBeta	HML	SMB	UMD
Mean	.003	.005	.002	.007
t-Stat	1.16	3.49	1.58	3.99
Sharpe	.022	.091	.004	.128
N	492	492	492	492

Panel B. Descriptive Statistics for Margin Requirements and the Monthly Intercept and Slopes of the SML Analogues from Multifactor Models

	Margin	Fama and French Three-Factor Model				Carhart Four-Factor Model				
		Intercept	Slopes			Intercept	Slopes			
			Market	HML	SMB		Market	HML	SMB	UMD
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	
Mean	0.613	0.008	0.003	0.004	0.004	0.009	0.002	0.004	0.003	0.002
STD (σ)	0.157	0.035	0.047	0.023	0.023	0.037	0.042	0.023	0.023	0.027
25 th	0.500	-0.009	-0.025	-0.009	-0.010	-0.011	-0.023	-0.009	-0.01	-0.012
Median	0.650	0.011	0.003	0.002	0.002	0.011	0.003	0.002	0.001	0.002
75 th	0.700	0.026	0.028	0.014	0.016	0.029	0.026	0.014	0.014	0.017

Table III, continued

Panel C. Descriptive Statistics for Control Variables

Control Variables	N	Mean	STD (σ)	Min	Max
$\Delta Mgn_Credit_{t-13, t-1}$	492	0.032	0.258	-0.759	0.716
$R_{mt} - R_{ft}$	492	0.007	0.047	-0.238	0.238
$R_{m, t-12, t-1}$	492	0.116	0.192	-0.492	0.760
$R_{m, t-36, t-13}$	492	0.274	0.294	-0.365	1.475
$Volatility_{m, t-12, t-1}$	492	0.008	0.003	0.003	0.020
$Skewness_{m, t-12, t-1}$	492	-0.434	0.764	-3.260	2.340
$Turnover_{t-12, t-1}$	492	0.550	0.172	0.245	1.054
P/D_{t-1}	492	24.493	6.854	11.529	37.468
$\Delta CPI_{t-13, t-1}$	492	0.034	0.037	-0.042	0.180
$\Delta M1_{t-13, t-1}$	492	0.000	0.004	-0.018	0.022
$\Delta IP_{t-13, t-1}$	492	0.051	0.117	-0.410	0.275

Table IV. Returns to the Factor Hedge Portfolios Before Changes in Margin Requirements

This table presents results from estimating Equation (1), as follows:

$$\text{Ret}_k_t = \alpha + \beta_1 \text{Mgn_Increase}_{t+3_t} + \beta_2 \text{Mgn_Increase}_{t+2_t} + \beta_3 \text{Mgn_Increase}_{t+1_t} + \beta_4 \text{Mgn_Decrease}_{t+3_t} + \beta_5 \text{Mgn_Decrease}_{t+2_t} + \beta_6 \text{Mgn_Decrease}_{t+1_t} + \text{Controls} + \varepsilon_t. \quad (1)$$

The dependent variable is the monthly return to each factor portfolio ($k = \text{MBeta, HML, SMB, or UMD}$), or the long leg or short leg for each hedge portfolio. The long leg of each portfolio includes high beta stocks, value stocks, small stocks, or winners. Each portfolio is held for one month and the portfolio return in month t is regressed on six dummy variables, along with the other controls, which are defined in Table II. The six dummy variables, **Increase (Decrease) $_{t+m}$** , $m = 1, 2, \text{ or } 3$, are assigned a value of 1 if there is a future increase (decrease) in margin requirements in month $t+m$. The sample period covers October 1934 through September 1975. All variables are defined in Table II. Robust t-ratios are provided in parentheses (Newey and West, 1987, with twelve monthly lags).

Dummy Variables for Future Returns	MBeta (1)	High Beta (2)	Low Beta (3)	HML (4)	Value (5)	Growth (6)	SMB (7)	Small (8)	Big (9)	UMD (10)	Winner (11)	Loser (12)
Mgn_Increase$_{t+3_t}$	0.020** (2.00)	0.030* (1.86)	0.011 (1.23)	0.024** (2.53)	0.037** (2.33)	0.013 (1.48)	0.001 (0.31)	0.025* (1.86)	0.023** (2.14)	-0.010 (-0.96)	0.018 (1.47)	0.028* (1.96)
Mgn_Increase$_{t+2_t}$	0.033*** (2.87)	0.051*** (2.92)	0.018** (2.54)	0.017*** (2.82)	0.046*** (3.48)	0.029** (2.29)	0.009 (1.39)	0.041*** (2.89)	0.032*** (3.06)	0.011* (1.92)	0.042*** (2.86)	0.031*** (2.93)
Mgn_Increase$_{t+1_t}$	0.041*** (5.41)	0.057*** (5.10)	0.016*** (2.64)	0.029*** (3.15)	0.053*** (3.58)	0.024*** (3.00)	0.017** (2.39)	0.044*** (3.48)	0.027*** (3.17)	-0.001 (-0.10)	0.035*** (3.33)	0.035*** (3.29)
Mgn_Decrease$_{t+1_t}$	-0.049*** (-3.06)	-0.065** (-2.54)	-0.016 (-1.38)	0.003 (0.40)	-0.045*** (-2.62)	-0.048** (-2.42)	-0.014 (-1.42)	-0.051*** (-2.65)	-0.037** (-2.28)	0.014 (0.91)	-0.042** (-2.22)	-0.056*** (-2.61)
Mgn_Decrease$_{t+2_t}$	-0.051** (-2.51)	-0.074** (-2.15)	-0.022 (-1.41)	-0.005 (-0.58)	-0.047* (-1.92)	-0.042 (-1.64)	-0.022** (-2.30)	-0.054* (-1.92)	-0.032 (-1.60)	0.001 (0.08)	-0.046* (-1.70)	-0.047* (-1.81)
Mgn_Decrease$_{t+3_t}$	-0.027** (-2.30)	-0.033* (-1.69)	-0.006 (-0.70)	-0.007 (-1.01)	-0.019 (-1.17)	-0.012 (-0.98)	-0.010** (-2.24)	-0.020 (-1.45)	-0.010 (-0.67)	0.014* (1.76)	-0.011 (-0.77)	-0.025* (-1.66)

Table IV, continued Control Variables	MBeta (1)	High Beta (2)	Low Beta (3)	HML (4)	Value (5)	Growth (6)	SMB (7)	Small (8)	Big (9)	UMD (10)	Winner (11)	Loser (12)
$\Delta \text{Mgn_Credit}_{t-13, t-1}$	-0.013** (-2.39)	-0.015* (-1.79)	-0.002 (-0.48)	-0.004* (-1.70)	-0.011* (-1.69)	-0.007 (-1.33)	-0.008*** (-3.10)	-0.013* (-1.89)	-0.004 (-0.93)	0.004* (1.69)	-0.007 (-1.28)	-0.011* (-1.85)
$R_{m, t-12, t-1}$	-0.001 (-0.16)	0.001 (0.11)	0.002 (0.55)	0.001 (0.66)	0.002 (0.35)	0.001 (0.12)	0.004* (1.86)	0.003 (0.58)	-0.001 (-0.18)	0.001 (0.28)	0.002 (0.44)	0.001 (0.26)
$R_{m, t-36, t-13}$	-0.006 (-1.64)	-0.008 (-1.38)	-0.002 (-0.76)	-0.001 (-0.88)	-0.007 (-1.41)	-0.005 (-1.42)	-0.003** (-2.45)	-0.007 (-1.59)	-0.004 (-0.97)	0.001 (0.47)	-0.004 (-1.13)	-0.005 (-1.19)
$\text{Volatility}_{m, t-12, t-1}$	-0.007 (-1.39)	-0.006 (-0.81)	0.001 (0.50)	-0.002 (-1.17)	-0.005 (-0.94)	-0.002 (-0.61)	-0.002 (-0.88)	-0.004 (-0.81)	-0.002 (-0.63)	0.000 (0.01)	-0.003 (-0.73)	-0.003 (-0.66)
$\text{Skewness}_{m, t-12, t-1}$	-0.003 (-0.78)	-0.001 (-0.22)	0.001 (0.61)	-0.002 (-0.95)	-0.002 (-0.47)	-0.000 (-0.11)	0.001 (0.46)	-0.001 (-0.20)	-0.001 (-0.42)	-0.000 (-0.19)	-0.001 (-0.19)	-0.000 (-0.09)
$\text{Turnover}_{t-12, t-1}$	0.004 (1.01)	0.000 (0.09)	-0.003 (-1.44)	-0.001 (-0.43)	-0.001 (-0.22)	-0.000 (-0.05)	0.000 (0.09)	-0.001 (-0.13)	-0.001 (-0.24)	-0.001 (-0.36)	-0.001 (-0.32)	-0.001 (-0.15)
P/D_{t-1}	-0.008*** (-2.88)	-0.011** (-2.51)	-0.003 (-1.23)	0.000 (0.18)	-0.006* (-1.69)	-0.006** (-2.10)	-0.002 (-1.31)	-0.007** (-1.97)	-0.005* (-1.77)	0.003** (2.06)	-0.005 (-1.62)	-0.008** (-2.41)
$\Delta \text{CPI}_{t-13, t-1}$	-0.009*** (-2.96)	-0.012*** (-2.83)	-0.003* (-1.65)	0.000 (0.35)	-0.007** (-2.45)	-0.008*** (-2.91)	-0.003*** (-2.65)	-0.009*** (-2.91)	-0.006** (-2.45)	0.002 (1.15)	-0.007*** (-2.82)	-0.009*** (-2.84)
$\Delta \text{M1}_{t-13, t-1}$	0.003 (1.50)	0.004 (1.44)	0.001 (0.88)	0.000 (0.21)	0.003 (1.35)	0.003 (1.49)	0.000 (0.19)	0.003 (1.33)	0.002 (1.48)	-0.000 (-0.42)	0.002 (1.19)	0.003 (1.30)
$\Delta \text{IP}_{t-13, t-1}$	0.000 (0.11)	-0.004 (-0.79)	-0.004* (-1.93)	0.003** (2.10)	-0.001 (-0.37)	-0.004 (-1.41)	-0.001 (-0.51)	-0.003 (-0.84)	-0.002 (-0.90)	0.001 (1.07)	-0.002 (-0.70)	-0.004 (-0.99)
Constant	0.004 (1.41)	0.013*** (3.44)	0.010*** (5.40)	0.003** (2.50)	0.013*** (4.40)	0.010*** (3.95)	0.002* (1.68)	0.012*** (4.11)	0.010*** (4.52)	0.006*** (5.01)	0.014*** (5.39)	0.008*** (2.75)
Adjusted R ²	0.04	0.05	0.04	0.04	0.05	0.05	0.03	0.05	0.04	0.00	0.05	0.05

Table V. Returns to the Factor Hedge Portfolios After Changes in Margin Requirements

This table presents results from estimating Equation (2), as follows:

$$\text{Ret}_k_t = \alpha + \beta_1 \text{Margin}_{t-1} + \text{Controls} + \varepsilon_t. \quad (2)$$

The dependent variable is the return in month t for each factor portfolio (i.e., MBeta, HML, SMB, or UMD), or the long leg or short leg for each hedge portfolio. The long leg of each hedge portfolio includes high beta stocks, value stocks, small stocks, or winners, respectively. Each portfolio is held for one month and the resulting portfolio return in month t is regressed on lagged margin requirements in month $t-1$, along with the other controls.

The top row presents the relevant results for the analysis of returns on each factor hedge portfolio. The second and third rows provide the analogous results for the long and short legs of each factor hedge portfolio. We only provide the coefficient of lagged margin requirements in each specification. The coefficients of the control variables are similar to those presented in Table IV, and are omitted for brevity. At the bottom of each column, we present the F-test (and its p-value) of the null hypothesis that the coefficient of lagged margin requirements is identical across the two regressions involving the long leg and the short leg, for each factor hedge portfolio. The sample covers the period, October 1934 through September 1975. Robust t-ratios are provided in parentheses beneath the parameter estimates (Newey and West, 1987, with twelve monthly lags).

Dependent Variable: Portfolio Return in month t	Coefficient of Lagged Margin Requirements			
	MBeta (1)	HML (2)	SMB (3)	UMD (4)
Hedge Portfolio	-0.05***	-0.04***	-0.02**	0.00
t-Stat	(-3.26)	(-3.81)	(-2.19)	(0.29)
Hedge Portfolio Adj. R ²	0.61	0.07	0.21	0.06
Long Leg	-0.05***	-0.04***	-0.03***	-0.02***
t-Stat	(-3.85)	(-4.49)	(-3.34)	(-2.86)
Long Leg Adj. R ²	0.83	0.82	0.84	0.89
Short Leg	-0.00	-0.00	-0.01***	-0.02***
t-Stat	(-0.21)	(-0.14)	(-2.69)	(-2.97)
Short Leg Adj. R ²	0.75	0.94	0.97	0.82
Controls	Yes	Yes	Yes	Yes
H ₀ : Long Leg = Short Leg p -value	-0.05*** (0.00)	-0.04*** (0.00)	-0.02** (0.03)	0.00 (0.77)

Table VI. Margin Requirements and Long Term Future Returns to Factor Hedge Portfolios

This table presents results from estimating Equation (2) and Equation (3), which analyze future returns to the factor hedge portfolios measured over the next month (t) following a change in margin requirements in month $t-1$, as well as longer term future returns measured over three-month intervals that span the next two years. This analysis requires that we construct our own hedge portfolio based on the market beta (MBeta), as well as replicating hedge portfolios that mimic the factors from Kenneth French's Data Library (HML, SMB, and UMD). Now the dependent variable is the future return on the replicating hedge portfolio based on each factor (i.e., MBeta, HML, SMB, or UMD in Panels A, B, C, and D, respectively), where every portfolio is held in month t , or over future three-month intervals that span the next two years covering months t to $t+23$. For each future three-month period, the resulting hedge portfolio returns are regressed on lagged margin requirements in month $t-1$ and the control variables used in Equation (2), which are defined in Table II. The sample covers October 1934 through September 1975. Robust t-ratios are provided in parentheses beneath the parameter estimates (Newey and West, 1987, with twelve monthly lags).

Panel A. Longer Term Future Returns to the MBeta Hedge Portfolio

Holding Period	Month	t	t+3	t+6	t+9	t+12	t+15	t+18	t+21
Variables	t	to t+2	to t+5	to t+8	to t+11	to t+14	to t+17	to t+20	to t+23
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
Margin_{t-1}	-0.05***	-0.19***	-0.23***	-0.18***	-0.15***	-0.13***	-0.06	-0.06	-0.02
	(-3.26)	(-4.87)	(-4.66)	(-4.16)	(-2.94)	(-3.13)	(-1.13)	(-1.15)	(-0.39)
Controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Adjusted R ²	0.61	0.38	0.12	0.09	0.07	0.08	0.08	0.05	0.02

Panel B. Longer Term Future Returns to the HML Hedge Portfolio

Holding Period	Month	t	t+3	t+6	t+9	t+12	t+15	t+18	t+21
Variables	t	to t+2	to t+5	to t+8	to t+11	to t+14	to t+17	to t+20	to t+23
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
Margin_{t-1}	-0.05***	-0.15***	-0.16***	-0.15***	-0.12***	-0.10***	-0.06*	-0.01	0.02
	(-3.98)	(-4.35)	(-4.83)	(-4.78)	(-3.81)	(-3.05)	(-1.80)	(-0.49)	(0.72)
Controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Adjusted R ²	0.07	0.14	0.11	0.08	0.10	0.08	0.09	0.05	0.04

Panel C. Longer Term Future Returns to the SMB Hedge Portfolio

Holding Period	Month	t	t+3	t+6	t+9	t+12	t+15	t+18	t+21
Variables	t	to t+2	to t+5	to t+8	to t+11	to t+14	to t+17	to t+20	to t+23
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
Margin_{t-1}	-0.04***	-0.12***	-0.13***	-0.13***	-0.12***	-0.10***	-0.09***	-0.06**	-0.05
	(-4.70)	(-4.21)	(-3.87)	(-4.28)	(-3.91)	(-3.83)	(-3.21)	(-2.26)	(-1.37)
Controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Adjusted R ²	0.15	0.19	0.06	0.06	0.07	0.09	0.14	0.10	0.08

Panel D. Longer Term Future Returns to the UMD Hedge Portfolio

Holding Period	Month	t	t+3	t+6	t+9	t+12	t+15	t+18	t+21
Variables	t	to t+2	to t+5	to t+8	to t+11	to t+14	to t+17	to t+20	to t+23
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
Margin_{t-1}	0.00	0.03	0.09	0.05	-0.00	0.07	0.08*	0.07	0.04
	(0.25)	(0.51)	(1.41)	(0.70)	(-0.03)	(1.17)	(1.96)	(1.62)	(0.63)
Controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Adjusted R ²	0.05	0.06	0.03	0.01	0.00	0.01	0.02	0.02	0.08

Table VII. Margin Requirements and the Monthly SML Intercept or Slope Coefficients from Multifactor Models

This table analyzes the relation between lagged margin requirements and the monthly intercept or slope coefficients of the security market line (SML) analogues for the factors in multifactor models. We begin by stratifying the set of NYSE stocks each month (t) according to the three factors in the Fama and French (1993) model, or the four factors in the Carhart (1997) model, to generate portfolios of test assets that vary along each dimension. We then examine the test assets using a two-stage regression approach. In the first stage, each month (t) we estimate the sensitivity of the returns from the set of test assets to every factor, and we then relate the cross section of returns on these test assets in month t to their estimated factor sensitivities, to obtain the monthly intercept and slope coefficients of the SML analogues for every factor. In the second stage, we estimate the time series relations specified in Equation (4) and Equation (5), between each of these monthly intercept or slope coefficients and lagged margin requirements, as well as the set of control variables. In columns (1) to (4) of Panel A, we provide the results from estimating Equations (4) and (5) based on the intercept or slope coefficients from the three-factor model. In columns (1) to (5) of Panel B, we present the analogous results for the four-factor model. Our sample period encompasses the 22 changes in margin requirements over the period, October 1934 to September 1975. All variables are defined in Table II. Robust t-ratios are provided in parentheses beneath the parameter estimates (Newey and West, 1987, with twelve monthly lags).

Panel A. Fama and French Three-Factor Model

Variables	Equation (4)	Equation (5)		
	Intercept	Slope Coefficients		
	(1)	Market (2)	HML (3)	SMB (4)
Margin_{t-1}	0.02* (1.83)	-0.03** (-2.51)	-0.03*** (-3.23)	-0.03*** (-3.13)
$\Delta\text{Mgn_Credit}_{t-13, t-1}$	0.00 (1.16)	-0.00* (-1.80)	-0.00 (-0.88)	-0.01*** (-3.42)
$R_{mt} - R_{ft}$	0.01*** (3.35)	0.04*** (8.29)	0.01*** (3.56)	0.01*** (7.84)
$R_{m, t-12, t-1}$	-0.00 (-0.58)	0.00 (0.92)	0.00 (1.05)	0.00*** (2.69)
$R_{m, t-36, t-13}$	0.00 (0.54)	-0.00 (-0.72)	-0.00 (-0.13)	-0.00 (-1.44)
$\text{Volatility}_{m, t-12, t-1}$	0.00 (0.89)	-0.00 (-0.91)	-0.00** (-2.00)	-0.00 (-0.68)
$\text{Skewness}_{m, t-12, t-1}$	0.00 (0.52)	-0.00 (-0.80)	-0.00 (-0.95)	0.00 (0.30)
$\text{Turnover}_{t-12, t-1}$	-0.00*** (-2.83)	0.01*** (3.24)	0.00 (1.03)	-0.00 (-1.04)
P/D_{t-1}	-0.00 (-0.03)	0.00 (0.05)	0.00 (0.80)	0.00*** (2.78)
$\Delta\text{CPI}_{t-13, t-1}$	-0.00 (-0.25)	0.00 (0.56)	0.00* (1.96)	-0.00 (-0.76)
$\Delta\text{M1}_{t-13, t-1}$	0.00 (0.33)	-0.00 (-0.72)	-0.00 (-0.11)	-0.00 (-0.20)
$\Delta\text{IP}_{t-13, t-1}$	-0.00 (-0.15)	-0.00 (-0.44)	0.00 (0.77)	-0.00 (-1.24)
Constant	-0.01 (-0.76)	0.02*** (2.72)	0.02*** (3.67)	0.02*** (3.53)
Adjusted R ²	0.13	0.55	0.10	0.28

Table VII, continued

Panel B. Carhart Four-Factor Model

Variables	Equation (4)	Equation (5)			
	Intercept	Slope Coefficients			
	(1)	Market	HML	SMB	UMD
	(1)	(2)	(3)	(4)	(5)
Margin_{t-1}	0.03** (2.46)	-0.03*** (-2.90)	-0.03*** (-3.75)	-0.02** (-2.01)	-0.01 (-0.75)
$\Delta\text{Mgn_Credit}_{t-13, t-1}$	0.00* (1.89)	-0.01*** (-2.83)	-0.00 (-0.63)	-0.00** (-2.50)	-0.00 (-0.06)
$R_{mt} - R_{ft}$	0.02*** (5.19)	0.03*** (7.40)	0.01*** (3.09)	0.01*** (6.79)	-0.00 (-1.43)
$R_{m, t-12, t-1}$	-0.00 (-0.92)	0.00 (1.31)	0.00 (0.72)	0.00 (1.56)	0.00** (2.51)
$R_{m, t-36, t-13}$	-0.00 (-0.26)	-0.00 (-0.26)	0.00 (0.14)	-0.00* (-1.85)	-0.00 (-0.58)
$\text{Volatility}_{m, t-12, t-1}$	0.00 (1.53)	-0.00* (-1.65)	-0.00 (-1.51)	-0.00 (-0.92)	-0.00 (-0.37)
$\text{Skewness}_{m, t-12, t-1}$	0.00 (1.26)	-0.00 (-1.45)	-0.00 (-1.11)	-0.00 (-0.11)	0.00 (0.39)
$\text{Turnover}_{t-12, t-1}$	-0.00* (-1.82)	0.00** (2.07)	0.00 (0.47)	0.00 (0.12)	-0.00 (-0.69)
P/D_{t-1}	-0.00 (-0.88)	0.00 (0.84)	0.00** (1.98)	0.00* (1.65)	0.00 (0.57)
$\Delta\text{CPI}_{t-13, t-1}$	0.00 (0.70)	-0.00 (-0.82)	0.00*** (2.82)	-0.00 (-0.48)	0.00 (1.31)
$\Delta\text{M1}_{t-13, t-1}$	-0.00 (-0.57)	0.00 (0.29)	-0.00 (-0.85)	0.00 (0.24)	-0.00 (-0.30)
$\Delta\text{IP}_{t-13, t-1}$	-0.00 (-0.33)	-0.00 (-0.24)	0.00 (0.22)	-0.00 (-0.20)	0.00 (1.02)
Constant	-0.01 (-1.22)	0.02*** (3.03)	0.02*** (4.20)	0.01** (2.35)	0.01 (1.00)
Adjusted R ²	0.25	0.48	0.11	0.27	0.03

Table VIII. Margin Requirements and the Monthly SML Intercept or Slope Coefficients Based on Alternative Test Assets

This table provides the results from estimating Equation (4) and Equation (5), using alternative sets of test assets to examine the relation between margin requirements and the monthly intercept or slope coefficients from the Fama and French (1993) three-factor and Carhart (1997) four-factor models, respectively. We follow the same methodology applied in Table VII. However, in Panel A we now use as our test assets the 25 value-weighted portfolios formed each month (t) from a two-way 5×5 independent sorting scheme based on book-to-market and firm size, to obtain the intercept and slope coefficients corresponding to each factor. In Panel B, we use as our test assets the Fama and French 49 industry portfolios every month (t), where we exclude industries with missing observations during our sample period. In each Panel, we once again regress the monthly intercept or slope coefficients from either the three-factor or four-factor model on the lagged value of margin requirements and the other controls. The control variables are defined in Table II, but their coefficients are omitted here for brevity. The sample period covers October 1934 through September 1975. Robust t-ratios are provided in parentheses beneath the parameter estimates (Newey and West, 1987, with twelve monthly lags).

Panel A. SML Intercepts and Slopes based on 25 Portfolios Formed on Book-to-Market and Size

Variables	Fama and French Three-Factor Model				
	Equation (4) Intercept	Equation (5) Slope Coefficients			
	(1)	Market (2)	HML (3)	SMB (4)	
Margin_{t-1}	0.06*** (3.26)	-0.06*** (-3.64)	-0.04*** (-4.05)	-0.03*** (-2.70)	
Controls	Yes	Yes	Yes	Yes	
Adjusted R ²	0.12	0.25	0.06	0.23	
	Carhart Four-Factor Model				
	Equation (4) Intercept	Equation (5) Slope Coefficients			
	(5)	Market (6)	HML (7)	SMB (8)	UMD (9)
Margin_{t-1}	0.05*** (2.71)	-0.05*** (-3.07)	-0.03*** (-3.49)	-0.03*** (-2.89)	0.02 (0.73)
Controls	Yes	Yes	Yes	Yes	Yes
Adjusted R ²	0.11	0.24	0.05	0.24	0.01

Table VIII, continued

Panel B. SML Intercepts and Slopes based on Fama and French 49 Industry Portfolios

Variables	Fama and French Three-Factor Model				
	Equation (4) Intercept	Equation (5) Slope Coefficients			
	(1)	Market (2)	HML (3)	SMB (4)	
Margin_{t-1}	0.03*** (2.62)	-0.03*** (-2.73)	-0.04*** (-4.33)	-0.03*** (-4.01)	
Controls	Yes	Yes	Yes	Yes	
Adjusted R ²	0.24	0.48	0.13	0.15	
Variables	Carhart Four-Factor Model				
	Equation (4) Intercept	Equation (5) Slope Coefficients			
	(5)	Market (6)	HML (7)	SMB (8)	UMD (9)
Margin_{t-1}	0.03** (2.19)	-0.03** (-2.24)	-0.04*** (-4.28)	-0.03*** (-4.15)	0.01 (0.77)
Controls	Yes	Yes	Yes	Yes	Yes
Adjusted R ²	0.23	0.47	0.13	0.16	0.00

Table IX. Margin Requirements, Future Returns, and Monthly SML Intercept or Slope Coefficients Based on Beta-Neutral Factor Hedge Portfolios

In Panel A of this table, we repeat the analysis in Table V and provide the results of estimating Equation (2), where we analyze future one-month-ahead returns to factor hedge portfolios that we construct to be market-neutral, based on HML, SMB, and UMD (labelled N-HML, N-SMB, and N-UMD, respectively). Similar to Table V, each market-neutral factor hedge portfolio is held for one month, and the resulting hedge portfolio return in month t is regressed on lagged margin requirements in month $t-1$ and the controls, which are defined in Table II.

In Panel B, we repeat the analysis in Table VII and provide the results of our second stage estimation of Equation (4) and Equation (5), using these beta-neutral factor hedge portfolios (N-HML, N-SMB, and N-UMD), rather than the analogous three factors from Kenneth French's Data Library. That is, we examine the relation between lagged margin requirements and the monthly SML intercept or slope coefficients from the three-factor model and the four-factor model, using these three beta-neutral factor portfolios. We analyze the same test assets and follow the same methodology applied in Table VII. The sample period covers October 1934 through September 1975. Robust t-ratios are provided in parentheses beneath the parameter estimates (Newey and West, 1987, with twelve monthly lags).

Panel A. Future Returns to the N-HML, N-SMB, and N-UMD Hedge Portfolios

One-month-ahead future returns Coefficient of Lagged Margin Requirements	Equation (2)		
	N-HML (1)	N-SMB (2)	N-UMD (3)
Margin_{t-1}	-0.05*** (-3.62)	-0.02*** (-3.08)	-0.01 (-0.38)
Controls	Yes	Yes	Yes
Adjusted R ²	0.05	0.04	0.00

Panel B. SML Intercepts and Slopes for the N-HML, N-SMB, and N-UMD Hedge Portfolios

Variables	Fama and French Three-Factor Model				
	Equation (4) Intercept	Equation (5) Slope Coefficients			
	(1)	Market	N-HML	N-SMB	
		(2)	(3)	(4)	
Margin_{t-1}	0.03** (2.48)	-0.05*** (-3.44)	-0.03*** (-2.89)	-0.01** (-2.07)	
Controls	Yes	Yes	Yes	Yes	
Adjusted R ²	0.17	0.56	0.03	0.04	
Variables	Carhart Four-Factor Model				
	Equation (4) Intercept	Equation (5) Slope Coefficients			
	(5)	Market	N-HML	N-SMB	N-UMD
		(6)	(7)	(8)	(9)
Margin_{t-1}	0.03** (2.20)	-0.04*** (-2.73)	-0.04*** (-4.43)	-0.02*** (-2.85)	-0.00 (-0.04)
Controls	Yes	Yes	Yes	Yes	Yes
Adjusted R ²	0.25	0.46	0.06	0.05	0.02

Table X. Controlling for the Cost of Leverage

In Panels A and B of this table, we estimate an expanded version of Equation (2) by adding a proxy for investors' cost of leverage to the specification. Our proxy is the call spread, defined as the difference between the broker's call money rate and the three-month Treasury Bill rate. For each factor, we analyze returns on the long leg and the short leg, as well as the hedge portfolio itself. For every regression we present the evidence for two specifications that include the lagged call spread, with and without lagged margin requirements. For brevity, we only provide the results for the main variables of interest, lagged margin requirements and the lagged call spread. In Panel A we present the results for MBeta and HML, and in Panel B we provide the results for SMB and UMD.

In Panels C and D, we present the results from estimating a similarly expanded version of Equation (4) and Equation (5) in the second stage of this analysis of the intercept and slope coefficients for the SML analogues of the factors from the three-factor and four-factor models. The sample period covers October 1934 through September 1975. Robust t-ratios are provided in parentheses beneath the parameter estimates (Newey and West, 1987, with twelve monthly lags).

Panel A. Future Returns to Long and Short Legs of the MBeta and HML Hedge Portfolios, as well as the Hedge Portfolios Themselves

One-month-ahead future returns Variables	Equation (1)						Equation (2)					
	MBeta (1)	Mbeta (2)	High Beta (3)	High Beta (4)	Low Beta (5)	Low Beta (6)	HML (7)	HML (8)	Value (9)	Value (10)	Growth (11)	Growth (12)
Margin _{t-1}		-0.05*** (-3.41)		-0.05*** (-4.03)		-0.00 (-0.07)		-0.04*** (-3.92)		-0.04*** (-4.74)		-0.00 (-0.18)
Call_Spread _{t-1}	-0.10 (-0.26)	-0.20 (-0.54)	0.05 (0.13)	-0.05 (-0.12)	0.15 (1.22)	0.15 (1.17)	0.07 (0.29)	-0.02 (-0.08)	0.03 (0.14)	-0.05 (-0.26)	-0.03 (-0.27)	-0.04 (-0.28)
Controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Adjusted R ²	0.61	0.61	0.83	0.83	0.75	0.75	0.05	0.07	0.82	0.82	0.94	0.94

Panel B. Future Returns to Long and Short Legs of the SMB and UMD Hedge Portfolios, as well as the Hedge Portfolios Themselves

One-month-ahead future returns Variables	Equation (1)						Equation (2)					
	SMB (1)	SMB (2)	Small (3)	Small (4)	Big (5)	Big (6)	UMD (7)	UMD (8)	Winner (9)	Winner (10)	Loser (11)	Loser (12)
Margin _{t-1}		-0.02** (-2.34)		-0.03*** (-3.55)		-0.01*** (-2.61)		0.00 (0.38)		-0.02*** (-2.85)		-0.02*** (-3.24)
Call_Spread _{t-1}	-0.13 (-0.62)	-0.18 (-0.81)	-0.06 (-0.24)	-0.12 (-0.51)	0.08 (1.08)	0.06 (0.85)	0.12 (0.65)	0.12 (0.68)	0.04 (0.23)	0.00 (0.02)	-0.07 (-0.39)	-0.12 (-0.64)
Controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Adjusted R ²	0.21	0.21	0.84	0.84	0.97	0.97	0.06	0.06	0.89	0.89	0.82	0.82

Table X, continued

Panel C. Intercepts and Slopes of the SML Analogues for the Fama and French Three-Factor Model

Variables	Equation (4) Intercept		Equation (5) Slope Coefficients					
			Market		HML		SMB	
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
Margin_{t-1}		0.02* (1.75)		-0.03** (-2.48)		-0.03*** (-3.32)		-0.03*** (-3.33)
Call_Spread _{t-1}	-0.29 (-0.91)	-0.24 (-0.77)	0.29 (0.88)	0.23 (0.70)	0.08 (0.38)	0.03 (0.13)	-0.11 (-0.60)	-0.17 (-0.91)
Controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Adjusted R ²	0.13	0.13	0.54	0.55	0.09	0.10	0.27	0.28

Panel D. Intercepts and Slopes of the SML Analogues for the Carhart Four-Factor Model

Variables	Equation (4) Intercept		Equation (5) Slope Coefficients							
			Market		HML		SMB		UMD	
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)
Margin_{t-1}		0.03** (2.52)		-0.04*** (-2.97)		-0.03*** (-3.90)		-0.02** (-2.02)		-0.01 (-0.78)
Call_Spread _{t-1}	-0.00 (-0.00)	0.06 (0.26)	-0.02 (-0.07)	-0.09 (-0.38)	0.03 (0.13)	-0.04 (-0.17)	-0.00 (-0.02)	-0.04 (-0.19)	-0.03 (-0.14)	-0.04 (-0.22)
Controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Adjusted R ²	0.25	0.25	0.48	0.48	0.09	0.11	0.26	0.27	0.03	0.03

Table XI. Controlling for Aggregate Disagreement or Short Sale Constraints

In Panels A and B of this table, we estimate an expanded version of Equation (2) by adding a measure of either aggregate disagreement or short sale constraints, along with its interaction with margin requirements. We consider three measures of aggregate disagreement in month t : (i) value weighted average idiosyncratic volatility (IV), (ii) value weighted aggregate share turnover across all stocks (TO), and (iii) the cross-sectional standard deviation of stock returns (Disp), along with one measure of market-wide short sale constraints: the aggregate short interest ratio (Short). In this analysis, we create a dummy variable (Disagree or Short) that equals one if our proxy for aggregate disagreement or short interest in the previous month ($t-1$) was above the median from the entire sample period, and zero otherwise. Here we provide the results for the main variable of interest, lagged margin requirements, along with the coefficients of the lagged dummy variable (Disagree or Short), along with its interaction with lagged margin requirements. Panel A provides the results for returns on the long and short legs of the MBeta and HML factor portfolios, as well as the hedge portfolios themselves, while Panel B provides the analogous results for the SMB and UMD factor portfolios.

In Panel C and D, we present the results from estimating an expanded version of Equations (4) and (5) in the second stage of this analysis of the intercepts and slopes of the SML analogues for the three-factor and four-factor models. We begin by repeating the first stage analysis applied in Table VII, to obtain the monthly intercept and SML slope coefficients from the three-factor and four-factor models, respectively. Then, for the second stage regression, we add a measure of aggregate disagreement (or short sale constraints), along with its interaction with margin requirements to the specifications in Equations (4) and (5). Panel C provides the results for the Fama and French (1993) three-factor model, and Panel D presents the results for the Carhart (1997) four-factor model. The sample period covers October 1934 through September 1975. Robust t-ratios are provided in parentheses beneath the parameter estimates (Newey and West, 1987, with twelve monthly lags).

Table XI, continued

Panel A. Future Returns to the Long and Short Legs of MBeta and HML Hedge Portfolios, as well as Hedge Portfolios Themselves

Equation (2) Variables	MBeta				High Beta				Low Beta			
	IV (1)	TO (2)	Disp (3)	Short (4)	IV (5)	TO (6)	Disp (7)	Short (8)	IV (9)	TO (10)	Disp (11)	Short (12)
Margin_{t-1}× Disagree/Short_{t-1}	-0.04** (-2.22)	0.01 (0.53)	0.05 (1.38)	0.01 (0.18)	-0.03* (-1.85)	0.02 (0.69)	0.06* (1.80)	0.02 (0.86)	0.01 (0.91)	0.00 (0.34)	0.01 (0.62)	0.02 (1.31)
Margin_{t-1} Disagree/Short _{t-1}	-0.03** (-2.20)	-0.05*** (-2.86)	-0.06*** (-2.99)	-0.05*** (-2.85)	-0.03** (-2.51)	-0.05*** (-3.08)	-0.06*** (-2.90)	-0.06*** (-3.54)	-0.00 (-0.72)	0.00 (0.08)	0.01 (0.80)	-0.01 (-0.93)
	0.03** (2.17)	-0.01 (-0.30)	-0.03 (-1.18)	-0.00 (-0.22)	0.03** (1.97)	-0.00 (-0.17)	-0.03 (-1.28)	-0.01 (-0.69)	-0.00 (-0.64)	0.00 (0.42)	0.00 (0.26)	-0.01 (-0.96)
Controls Adjusted R ²	Yes 0.61	Yes 0.61	Yes 0.61	Yes 0.61	Yes 0.83	Yes 0.83	Yes 0.83	Yes 0.83	Yes 0.75	Yes 0.75	Yes 0.75	Yes 0.75
Equation (2) Variables	HML				Value				Growth			
	IV (13)	TO (14)	Disp (15)	Short (16)	IV (17)	TO (18)	Disp (19)	Short (20)	IV (21)	TO (22)	Disp (23)	Short (24)
Margin_{t-1}× Disagree/Short_{t-1}	-0.00 (-0.37)	-0.00 (-0.10)	0.02 (0.77)	-0.00 (-0.14)	-0.01 (-1.14)	0.01 (0.58)	0.04 (1.45)	0.01 (0.80)	-0.01 (-1.23)	0.01 (1.24)	0.02 (1.57)	0.01 (1.29)
Margin_{t-1} Disagree/Short _{t-1}	-0.04*** (-3.40)	-0.04*** (-3.04)	-0.04*** (-2.62)	-0.04*** (-3.43)	-0.03*** (-3.46)	-0.04*** (-3.35)	-0.05*** (-2.83)	-0.05*** (-4.41)	0.00 (0.52)	-0.00 (-0.81)	-0.00 (-0.74)	-0.01 (-0.89)
	0.01 (0.63)	0.01 (0.54)	-0.01 (-0.54)	0.00 (0.28)	0.01 (1.29)	-0.00 (-0.01)	-0.02 (-1.00)	-0.01 (-0.57)	0.01 (1.09)	-0.01 (-1.04)	-0.01 (-1.49)	-0.01 (-1.12)
Controls Adjusted R ²	Yes 0.07	Yes 0.07	Yes 0.07	Yes 0.07	Yes 0.82	Yes 0.83	Yes 0.83	Yes 0.82	Yes 0.94	Yes 0.94	Yes 0.94	Yes 0.94

Table XI, continued

Panel B. Future Returns to the Long and Short Legs of SMB and UMD Hedge Portfolios, as well as Hedge Portfolios Themselves

Equation (2) Variables	SMB				Small				Big			
	IV (1)	TO (2)	Disp (3)	Short (4)	IV (5)	TO (6)	Disp (7)	Short (8)	IV (9)	TO (10)	Disp (11)	Short (12)
Margin_{t-1}× Disagree/Short_{t-1}	-0.01 (-1.11)	0.02 (1.12)	0.04* (1.81)	0.03** (2.06)	-0.02 (-1.45)	0.02 (0.93)	0.04* (1.75)	0.03* (1.83)	-0.00 (-1.24)	-0.00 (-0.30)	0.00 (0.54)	-0.00 (-0.55)
Margin_{t-1} Disagree/Short _{t-1}	-0.01 (-1.25)	-0.02* (-1.96)	-0.02 (-1.57)	-0.03*** (-3.15)	-0.02** (-2.04)	-0.03*** (-2.59)	-0.03** (-2.28)	-0.04*** (-3.88)	-0.01** (-2.28)	-0.01** (-2.25)	-0.01** (-2.53)	-0.01** (-2.40)
	0.01 (1.32)	-0.01 (-0.51)	-0.01 (-1.14)	-0.02** (-2.23)	0.01 (1.62)	-0.01 (-0.35)	-0.02 (-1.13)	-0.02* (-1.76)	0.00 (1.19)	0.00 (0.44)	-0.00 (-0.67)	0.00 (1.38)
Controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Adjusted R ²	0.21	0.22	0.22	0.22	0.84	0.84	0.84	0.84	0.97	0.97	0.97	0.97
Equation (2) Variables	UMD				Winner				Loser			
	IV (13)	TO (14)	Disp (15)	Short (16)	IV (17)	TO (18)	Disp (19)	Short (20)	IV (21)	TO (22)	Disp (23)	Short (24)
Margin_{t-1}× Disagree/Short_{t-1}	0.00 (0.08)	-0.05** (-2.04)	-0.06* (-1.92)	-0.00 (-0.13)	-0.01 (-0.67)	-0.01 (-1.08)	0.00 (0.04)	0.02 (1.23)	-0.01 (-0.70)	0.03* (1.70)	0.06** (2.31)	0.02 (1.41)
Margin_{t-1} Disagree/Short _{t-1}	0.00 (0.17)	0.02* (1.92)	0.03* (1.81)	0.00 (0.28)	-0.02** (-2.10)	-0.01 (-1.10)	-0.01 (-0.98)	-0.02*** (-2.78)	-0.02* (-1.86)	-0.03*** (-3.08)	-0.04** (-2.47)	-0.03*** (-3.25)
	-0.00 (-0.08)	0.03** (2.29)	0.04* (1.92)	0.00 (0.20)	0.01 (0.84)	0.02* (1.92)	0.01 (0.79)	-0.01 (-1.06)	0.01 (0.82)	-0.02 (-1.30)	-0.03* (-1.84)	-0.01 (-1.16)
Controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Adjusted R ²	0.06	0.07	0.07	0.06	0.89	0.90	0.90	0.89	0.82	0.82	0.83	0.82

Table XI, continued

Panel C. Intercepts and Slopes of SML Analogues for Fama and French Three-Factor Model

Variables	Equation (4) Intercept				Equation (5) Market Slope			
	IV (1)	TO (2)	Disp (3)	Short (4)	IV (5)	TO (6)	Disp (7)	Short (8)
Margin_{t-1}× Disagree/Short_{t-1}	0.01 (0.64)	0.01 (0.25)	-0.01 (-0.50)	0.00 (0.05)	-0.02 (-0.93)	0.00 (0.16)	0.02 (1.00)	0.00 (0.11)
Margin_{t-1} Disagree/Short _{t-1}	0.02 (1.46)	0.02* (1.67)	0.04*** (2.74)	0.02 (1.53)	-0.02** (-2.03)	-0.03** (-2.42)	-0.05*** (-3.44)	-0.03** (-2.24)
Disagree/Short _{t-1}	-0.01 (-0.44)	-0.00 (-0.19)	0.01 (0.86)	-0.01 (-0.35)	0.01 (0.81)	-0.00 (-0.10)	-0.02 (-1.18)	0.00 (0.05)
Controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Adjusted R ²	0.13	0.13	0.13	0.13	0.55	0.55	0.55	0.55
Variables	Equation (5) HML Slope				Equation (5) SMB Slope			
	IV (9)	TO (10)	Disp (11)	Short (12)	IV (13)	TO (14)	Disp (15)	Short (16)
Margin_{t-1}× Disagree/Short_{t-1}	-0.01 (-0.51)	0.01 (0.50)	0.02 (1.53)	0.02 (1.40)	-0.01 (-0.69)	0.02 (1.39)	0.02 (1.61)	0.03** (2.24)
Margin_{t-1} Disagree/Short _{t-1}	-0.02*** (-2.64)	-0.03*** (-2.59)	-0.03** (-2.53)	-0.03*** (-3.20)	-0.02** (-2.22)	-0.03*** (-2.83)	-0.03** (-2.16)	-0.04*** (-3.80)
Disagree/Short _{t-1}	0.00 (0.34)	-0.00 (-0.23)	-0.01 (-1.14)	-0.01 (-1.06)	0.01 (0.76)	-0.01 (-0.68)	-0.01 (-1.05)	-0.02** (-2.02)
Controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Adjusted R ²	0.10	0.10	0.10	0.10	0.28	0.29	0.29	0.28

Table XI, continued

Panel D. Intercepts and Slopes of SML Analogues for Carhart Four-Factor Model

Variables	Equation (4) Intercept				Equation (5) Market Slope			
	IV (1)	TO (2)	Disp (3)	Short (4)	IV (5)	TO (6)	Disp (7)	Short (8)
Margin_{t-1}× Disagree/Short_{t-1}	0.01 (0.49)	-0.02 (-0.83)	-0.01 (-0.40)	-0.00 (-0.23)	-0.01 (-0.58)	0.02 (1.07)	0.02 (0.76)	0.01 (0.57)
Margin_{t-1}	0.03** (2.06)	0.04*** (2.70)	0.03** (2.47)	0.03** (2.38)	-0.03** (-2.38)	-0.04*** (-3.06)	-0.04*** (-2.86)	-0.04*** (-2.87)
Disagree/Short _{t-1}	-0.01 (-0.49)	0.01 (0.93)	0.01 (0.40)	-0.00 (-0.01)	0.01 (0.65)	-0.02 (-1.14)	-0.01 (-0.66)	-0.01 (-0.36)
Controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Adjusted R ²	0.25	0.25	0.25	0.25	0.48	0.49	0.48	0.48
Variables	Equation (5) HML Slope				Equation (5) SMB Slope			
	IV (9)	TO (10)	Disp (11)	Short (12)	IV (13)	TO (14)	Disp (15)	Short (16)
Margin_{t-1}× Disagree/Short_{t-1}	-0.01 (-1.22)	0.00 (0.28)	0.01 (0.89)	0.00 (0.32)	-0.01 (-0.49)	0.02* (1.84)	0.03** (2.20)	0.02 (1.64)
Margin_{t-1}	-0.03*** (-3.49)	-0.03*** (-3.35)	-0.03*** (-3.12)	-0.03*** (-3.41)	-0.02 (-1.50)	-0.02** (-2.25)	-0.02* (-1.87)	-0.03** (-2.38)
Disagree/Short _{t-1}	0.01 (1.33)	-0.00 (-0.01)	-0.01 (-0.68)	-0.01 (-0.54)	0.01 (0.66)	-0.01 (-1.13)	-0.02 (-1.54)	-0.02* (-1.81)
Controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Adjusted R ²	0.11	0.11	0.11	0.11	0.27	0.28	0.28	0.27
Variables	Equation (5) UMD Slope							
	IV (17)	TO (18)	Disp (19)	Short (20)				
Margin_{t-1}× Disagree/Short_{t-1}	-0.00 (-0.21)	-0.02 (-1.11)	-0.01 (-0.70)	0.01 (0.39)				
Margin_{t-1}	-0.01 (-0.56)	0.00 (0.16)	-0.01 (-0.44)	-0.01 (-0.86)				
Disagree/Short _{t-1}	0.00 (0.38)	0.02 (1.06)	0.01 (0.49)	-0.01 (-0.53)				
Controls	Yes	Yes	Yes	Yes				
Adjusted R ²	0.03	0.03	0.03	0.03				